

Superoptimization

How fast can your code go?

James Pallister
University of Bristol & Embecosm

What is superoptimization?



Unoptimized
code

What is superoptimization?



Unoptimized
code



Compiler
optimized
code

What is superoptimization?



Unoptimized
code



Compiler
optimized
code



Superoptimized
code

Plan for today

What is superoptimization?



Latest developments



The GNU Superoptimizer



Plan for today

What is superoptimization?



Latest developments

NEW

The GNU Superoptimizer



Superoptimization in action

```
int sign(int n)
{
    if(n > 0)
        return 1;
    else if(n < 0)
        return -1;
    else
        return 0;
}
```

Superoptimization in action

```
int sign(int n)
{
    if(n > 0)
        return 1;
    else if(n < 0)
        return -1;
    else
        return 0;
}
```


Superoptimization in action

```
int sign(int n)
{
    if(n > 0)
        return 1;
    else if(n < 0)
        return -1;
    else
        return 0;
}
```

```
    cmp.l   d0, 0
    ble     L1
    move.l  d1, 1
    bra     L3
L1:
    bge     L2
    move.l  d1, -1
    bra     L3
L2:
    move.l  d1, 0
L3:
```

Superoptimization in action

```
int sign(int n)
{
    if(n > 0)
        return 1;
    else if(n < 0)
        return -1;
    else
        return 0;
}
```

```
add.l  d0, d0
subx.l d1, d1
negx.l d0
addx.l d1, d1
```

Superoptimization in action

```
int sign(int n)           cmp.l  d0, 0           add.l  d0, d0
{
    if(n > 0)             ble   L1           subx.l d1, d1
        return 1;        move.l d1, 1         negx.l d0
    else if(n < 0)       bra   L3           addx.l d1, d1
        return -1;
    else
        return 0;
}

L1:
    bge   L2
    move.l d1, -1
    bra   L3
L2:
    move.l d1, 0
L3:
```

How does it work?

d0 ← n

add.l d0, d0

subx.l d1, d1

negx.l d0

addx.l d1, d1

d1 → sign(n)

How does it work?

`d0 ← n`

`add.l d0, d0`

`subx.l d1, d1`

`negx.l d0`

`addx.l d1, d1`

`d1 → sign(n)`

x	d0	d1
---	----	----

0	-3	
---	----	--

x	d0	d1
---	----	----

0	0	
---	---	--

x	d0	d1
---	----	----

0	2	
---	---	--

How does it work?

`d0 ← n`

`add.l d0, d0`

`subx.l d1, d1`

`negx.l d0`

`addx.l d1, d1`

`d1 → sign(n)`

x	d0	d1
---	----	----

0	-3	
---	----	--

1	-6	
---	----	--

x	d0	d1
---	----	----

0	0	
---	---	--

0	0	
---	---	--

x	d0	d1
---	----	----

0	2	
---	---	--

0	4	
---	---	--

How does it work?

`d0 ← n`

`add.l d0, d0`

`subx.l d1, d1`

`negx.l d0`

`addx.l d1, d1`

`d1 → sign(n)`

x	d0	d1
---	----	----

0	-3	
---	----	--

1	-6	
---	----	--

0	-6	-1
---	----	----

x	d0	d1
---	----	----

0	0	
---	---	--

0	0	
---	---	--

0	0	0
---	---	---

x	d0	d1
---	----	----

0	2	
---	---	--

0	4	
---	---	--

0	4	0
---	---	---

How does it work?

d0 ← n

add.l d0, d0

subx.l d1, d1

negx.l d0

addx.l d1, d1

d1 → sign(n)

x	d0	d1
---	----	----

0	-3	
---	----	--

1	-6	
---	----	--

0	-6	-1
---	----	----

1	6	-1
---	---	----

x	d0	d1
---	----	----

0	0	
---	---	--

0	0	
---	---	--

0	0	0
---	---	---

0	0	0
---	---	---

x	d0	d1
---	----	----

0	2	
---	---	--

0	4	
---	---	--

0	4	0
---	---	---

1	-4	0
---	----	---

How does it work?

d0 ← n

add.l d0, d0

subx.l d1, d1

negx.l d0

addx.l d1, d1

d1 → sign(n)

x	d0	d1
---	----	----

0	-3	
---	----	--

1	-6	
---	----	--

0	-6	-1
---	----	----

1	6	-1
---	---	----

0	6	-1
---	---	----

x	d0	d1
---	----	----

0	0	
---	---	--

0	0	
---	---	--

0	0	0
---	---	---

0	0	0
---	---	---

0	0	0
---	---	---

x	d0	d1
---	----	----

0	2	
---	---	--

0	4	
---	---	--

0	4	0
---	---	---

1	-4	0
---	----	---

0	-4	1
---	----	---

How does it work?

d0 ← n

add.l d0, d0

subx.l d1, d1

negx.l d0

addx.l d1, d1

d1 → sign(n)

x	d0	d1
---	----	----

0	-3	
---	----	--

1	-6	
---	----	--

0	-6	-1
---	----	----

1	6	-1
---	---	----

0	6	-1
---	---	----

-1

x	d0	d1
---	----	----

0	0	
---	---	--

0	0	
---	---	--

0	0	0
---	---	---

0	0	0
---	---	---

0	0	0
---	---	---

0

x	d0	d1
---	----	----

0	2	
---	---	--

0	4	
---	---	--

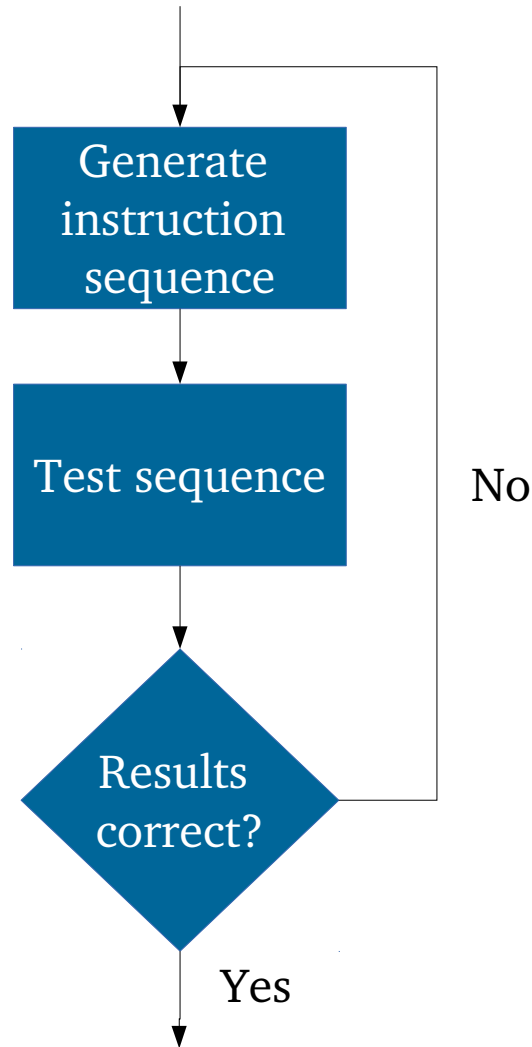
0	4	0
---	---	---

1	-4	0
---	----	---

0	-4	1
---	----	---

1

“A look at the smallest program”



A recent example: Atmel AVR

A recent example: Atmel AVR

Is x a power of 2?

A recent example: Atmel AVR

Is x a power of 2?

```
r = !((x-1) & x) && x;
```

A recent example: Atmel AVR

Is x a power of 2?

```
r = !((x-1) & x) && x;
```

Compiled code

```
mov    r20, r24
ldi    r21, 0
mov    r22, r20
mov    r19, r21
subi   r22, 1
sbc    r19, r1
and    r22, r20
and    r19, r21
or     r22, r19
brne   .+0
ldi    r25, 0x01
cpse   r24, 1
rjmp   .+0
ldi    r25, 0
mov    r24, r25
ret
ldi    r24, 0
ret
```

A recent example: Atmel AVR

Is x a power of 2?

```
r = !((x-1) & x) && x;
```

Compiled code

```
mov    r20, r24
ldi    r21, 0
mov    r22, r20
mov    r19, r21
subi   r22, 1
sbc    r19, r1
and    r22, r20
and    r19, r21
or     r22, r19
brne   .+0
ldi    r25, 0x01
cpse   r24, 1
rjmp   .+0
ldi    r25, 0
mov    r24, r25
ret
ldi    r24, 0
ret
```

Superoptimized code

```
mov    r1, r0
dec    r1
eor    r0, r1
sub    r1, r0
adc    r1, r1
and    r1, r0
ret
```


Superoptimization fundamentals: Enumeration

Superoptimization fundamentals: Enumeration

Generating the sequences of instructions

Superoptimization fundamentals: Enumeration

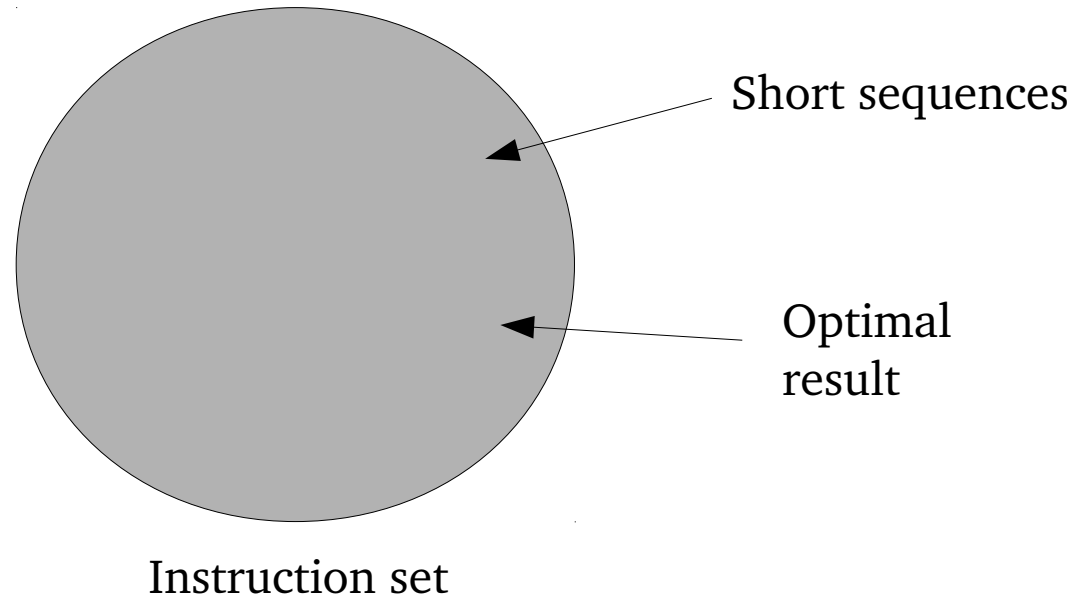
Generating the sequences of instructions

- But doing them all takes far too long

Superoptimization fundamentals: Enumeration

Generating the sequences of instructions

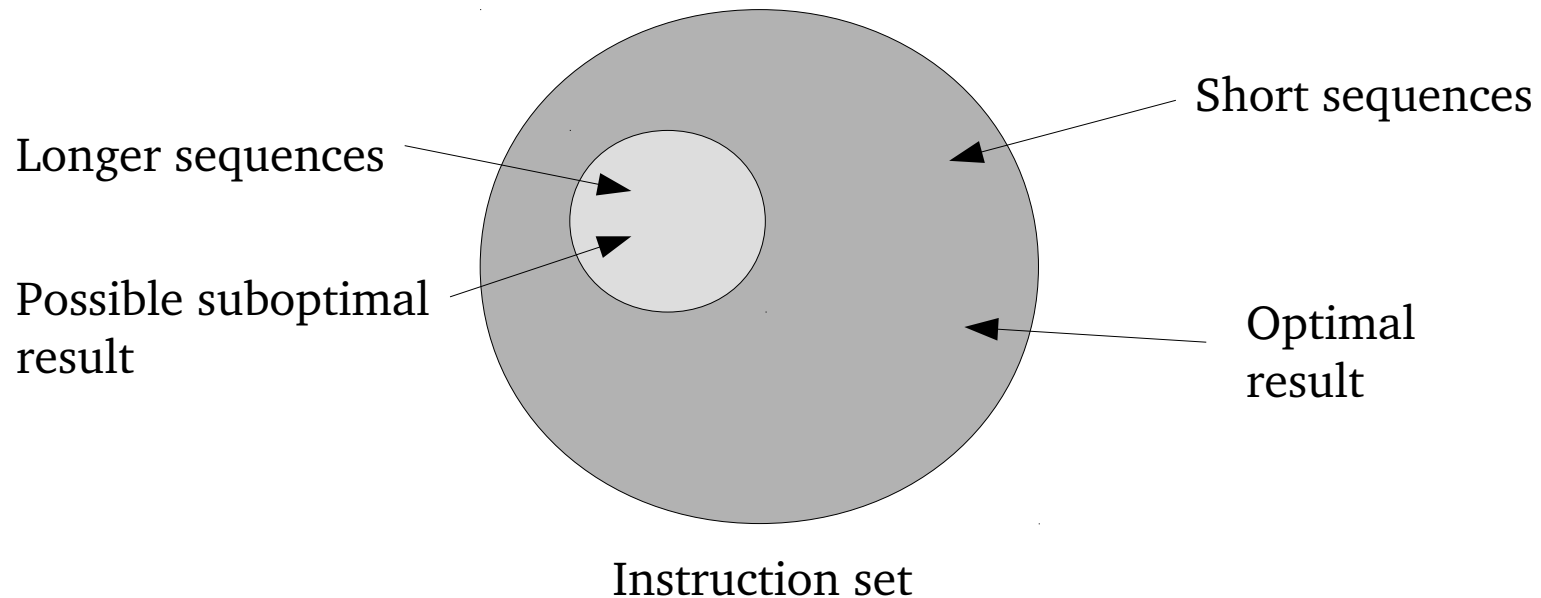
- But doing them all takes far too long



Superoptimization fundamentals: Enumeration

Generating the sequences of instructions

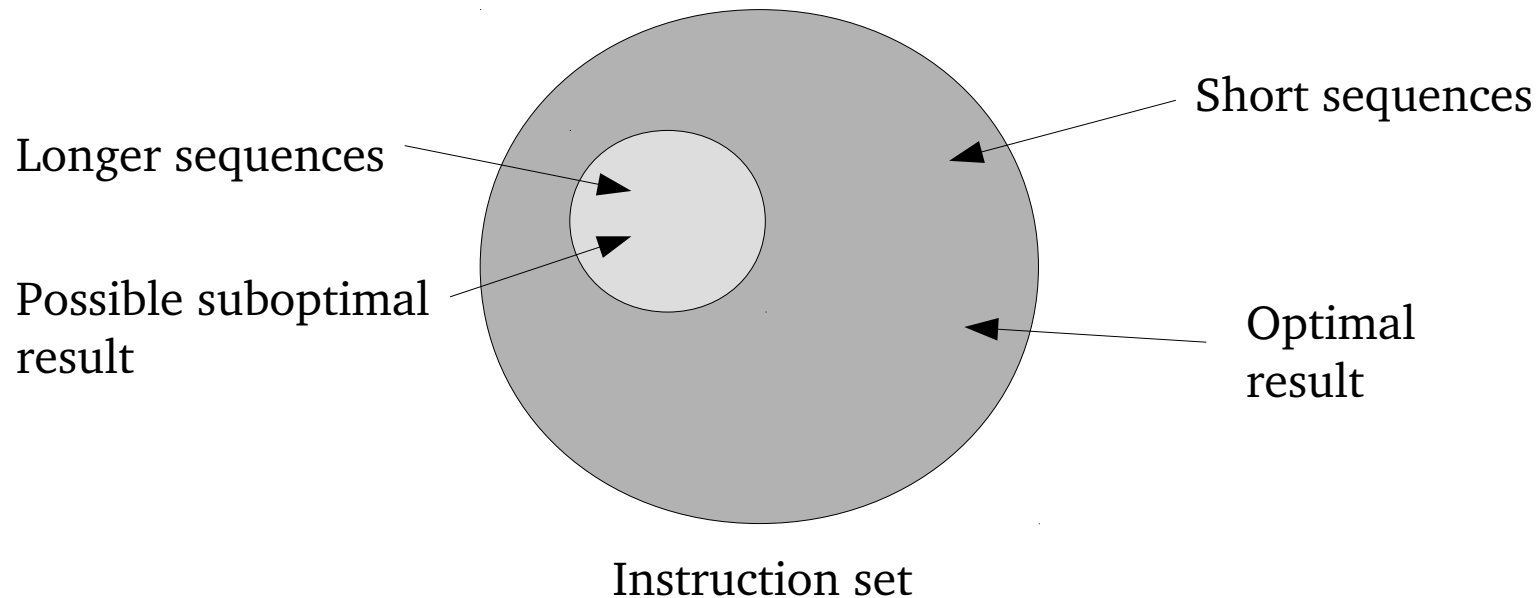
- But doing them all takes far too long



Superoptimization fundamentals: Enumeration

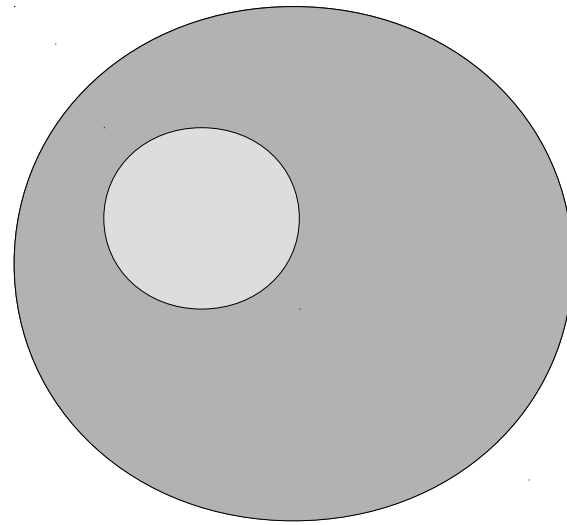
Generating the sequences of instructions

- But doing them all takes far too long



How to select the sequences of instructions?

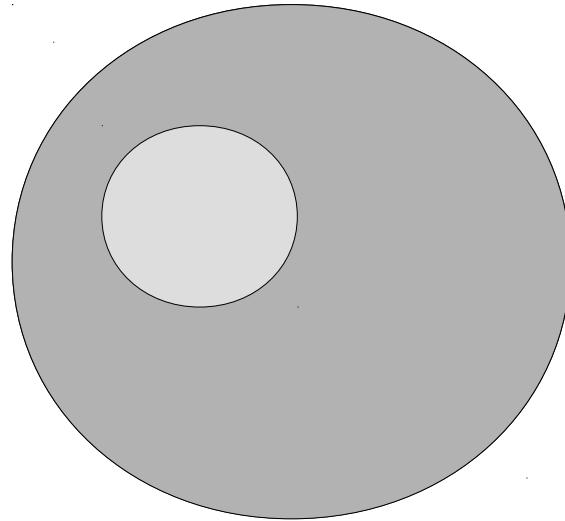
Superoptimization fundamentals: Pruning



Instruction set

Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

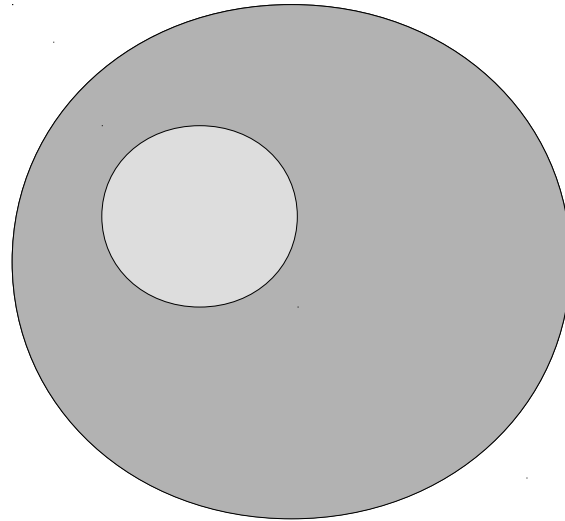


Instruction set

Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

How do we quickly ignore bad sequences?

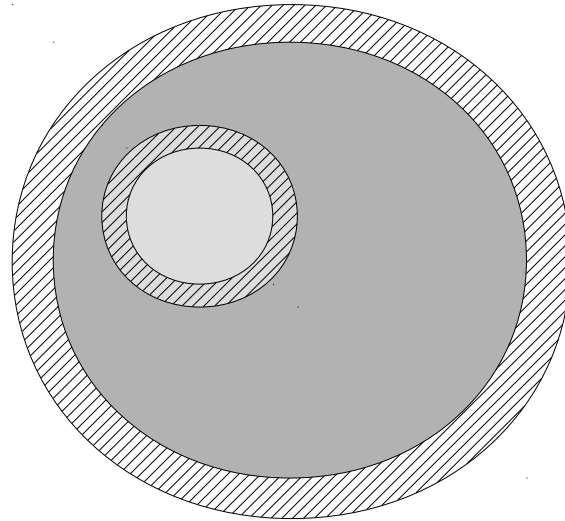


Instruction set

Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

How do we quickly ignore bad sequences?



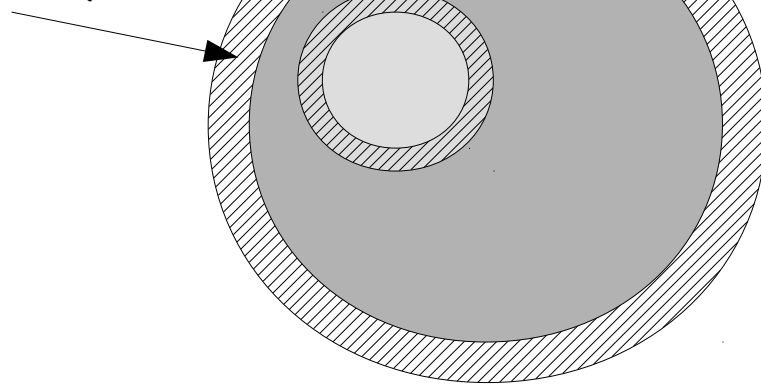
Instruction set

Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

How do we quickly ignore bad sequences?

Register renaming
`add r0,r1 = add r2,r3`

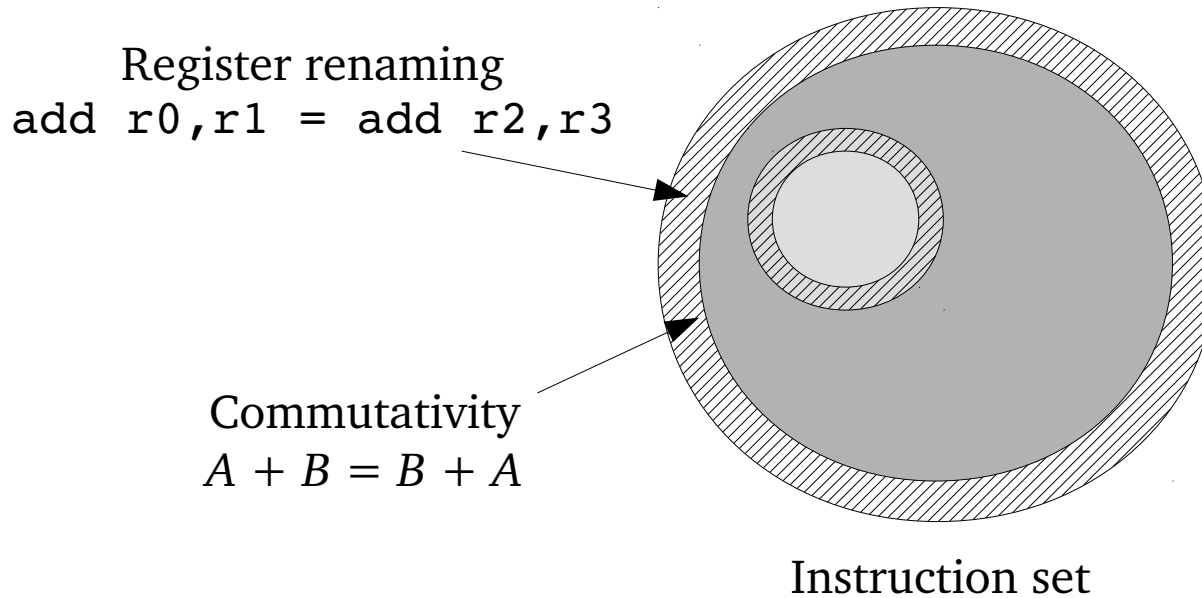


Instruction set

Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

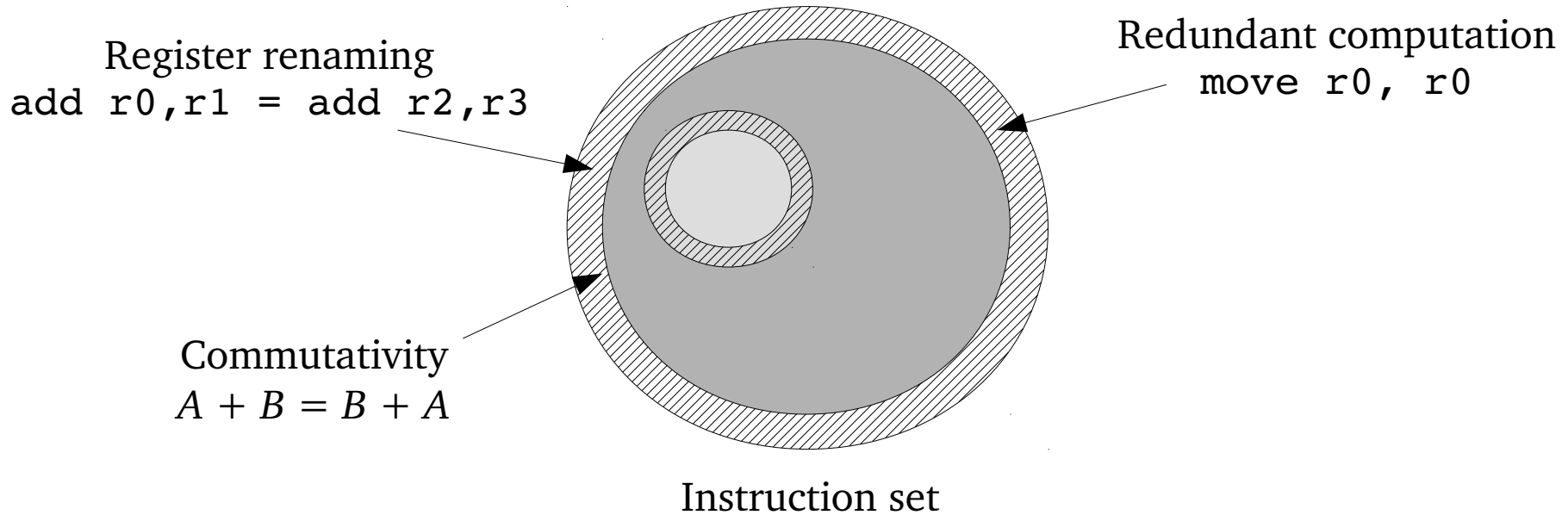
How do we quickly ignore bad sequences?



Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

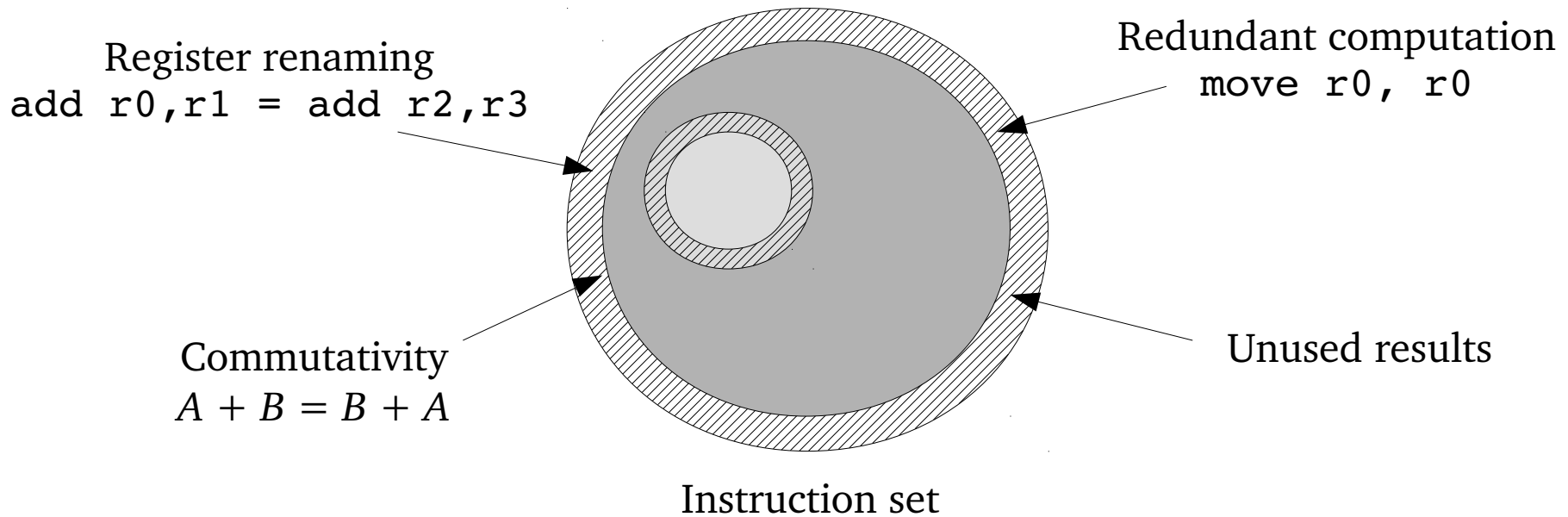
How do we quickly ignore bad sequences?



Superoptimization fundamentals: Pruning

Not all instruction sequences are valid.

How do we quickly ignore bad sequences?



Superoptimization fundamentals: Testing

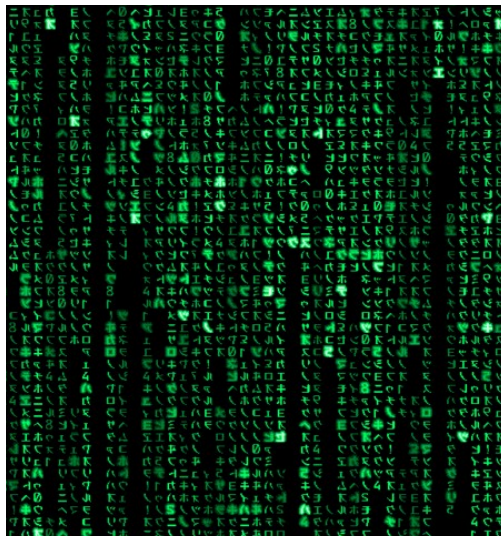
Superoptimization fundamentals: Testing

Is the sequence correct?

Superoptimization fundamentals: Testing

Is the sequence correct?

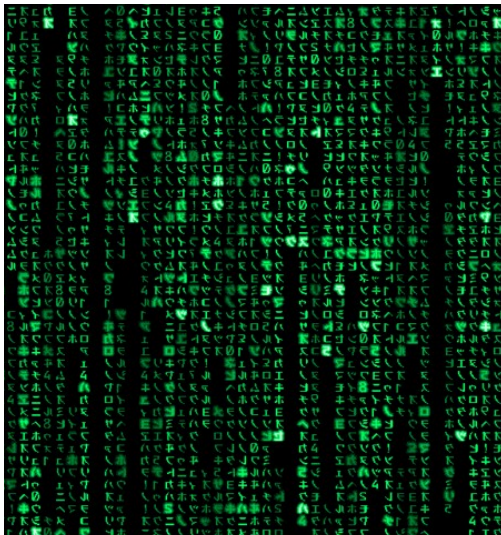
Testing
(simulation)



Superoptimization fundamentals: Testing

Is the sequence correct?

Testing
(simulation)



Mathematical proof
(symbolic solving)

5	3			7			
6			1	9	5		
	9	8					6
8							3
4							1
							6
							5
			8			7	9

Overlaying mathematical identities:

- $0x = 0$
- $xx = x$
- $x\bar{x} = 0$
- $xy = yx$
- $(xy)z = x(yz)$
- $x+(y+z) = x+y+z$
- $x(x+y) = x$
- $1+x = 1$
- $x+x = x$
- $x+\bar{x} = 1$
- $x+y = y+x$
- $(x+y)+z = x+(y+z)$
- $x(y+z) = xy+xz$
- $x+xy = x$

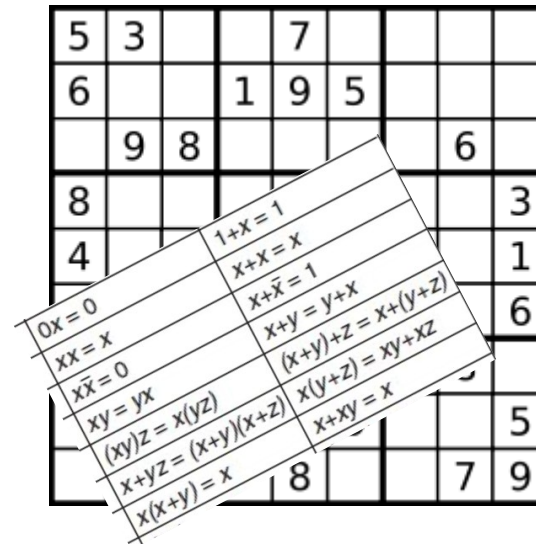
Superoptimization fundamentals: Testing

Is the sequence correct?

Testing
(simulation)



Mathematical proof
(symbolic solving)



1. Choose some input
2. Run/simulate
3. Check output

Superoptimization fundamentals: Testing

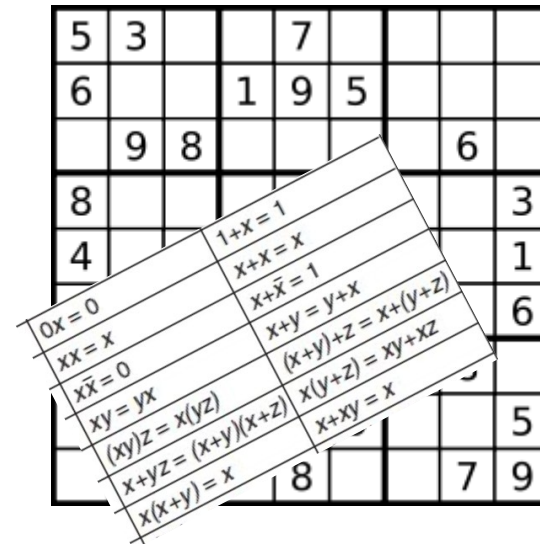
Is the sequence correct?

Testing
(simulation)



1. Choose some input
2. Run/simulate
3. Check output

Mathematical proof
(symbolic solving)

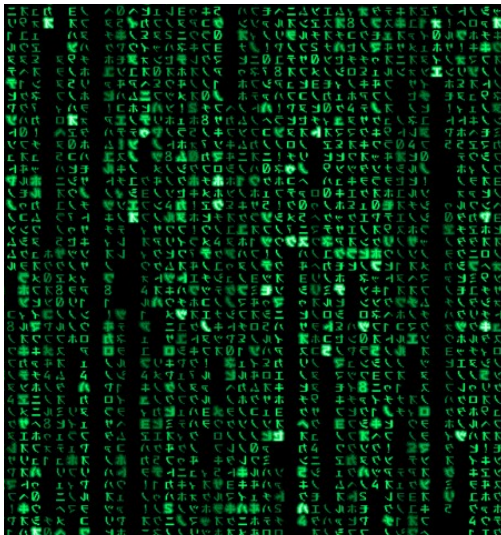


Formal verification
Proves the sequence correct
Slow

Superoptimization fundamentals: Testing

Is the sequence correct?

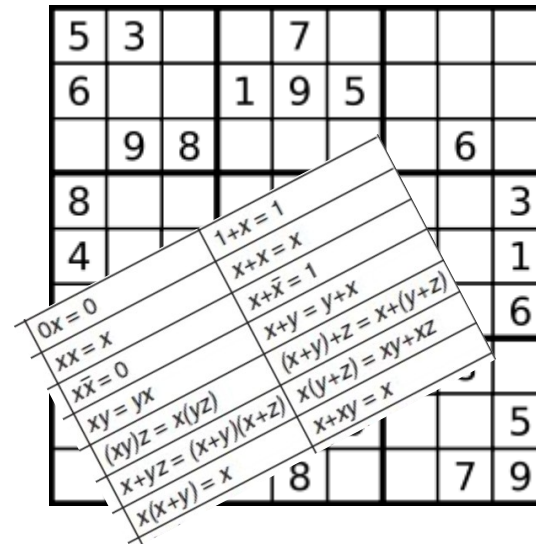
Testing
(simulation)



Use Both

1. Choose some input
2. Run/simulate
3. Check output

Mathematical proof
(symbolic solving)



Formal verification
Proves the sequence correct
Slow

Superoptimization fundamentals: Costing

Superoptimization fundamentals: Costing

Which sequence is the best?

Superoptimization fundamentals: Costing

Which sequence is the best?

Execution time



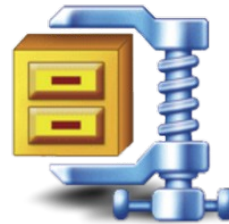
Superoptimization fundamentals: Costing

Which sequence is the best?

Execution time



Code size



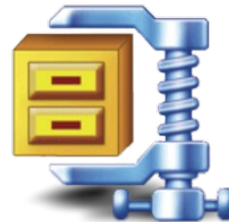
Superoptimization fundamentals: Costing

Which sequence is the best?

Execution time



Code size



Energy consumption



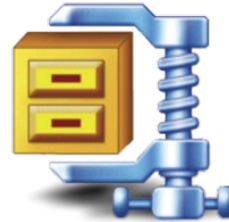
Superoptimization fundamentals: Costing

Which sequence is the best?

Execution time



Code size



Energy consumption



If you can enumerate the instructions in cost order, the first correct sequence is the optimal sequence.

Plan for today

What is superoptimization?



Latest developments

NEW

The GNU Superoptimizer



Search space pruning

Search space pruning

Restrict parameters

- Registers
 - 50% of instruction sequences of length 8 use less than 4 registers
- Immediate constants
 - Frequently used constants: -16 to +16, 2^n , 2^{n-1}

Search space pruning

Restrict parameters

- Registers
 - 50% of instruction sequences of length 8 use less than 4 registers
- Immediate constants
 - Frequently used constants: -16 to +16, 2^n , 2^n-1

Remove meaningless constructs

- `mov r0, r0`
- `add r0, r0, #0`

Search space pruning

Restrict parameters

- Registers
 - 50% of instruction sequences of length 8 use less than 4 registers
- Immediate constants
 - Frequently used constants: -16 to +16, 2^n , 2^n-1

Remove meaningless constructs

- `mov r0, r0`
- `add r0, r0, #0`

Canonical form

Canonical form

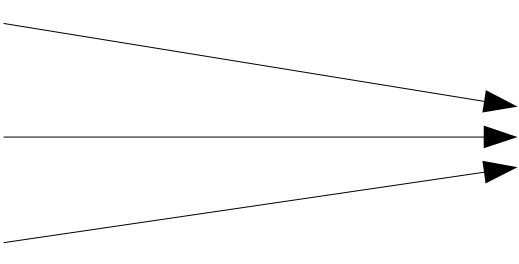
`mov r1, r0` has many equivalent versions

Canonical form

`mov r1, r0` has many equivalent versions

Rename each register so they appear in sequence:

`mov r1, r0`
`mov r4, r2`
`mov r2, r8`



`mov r1, r0`

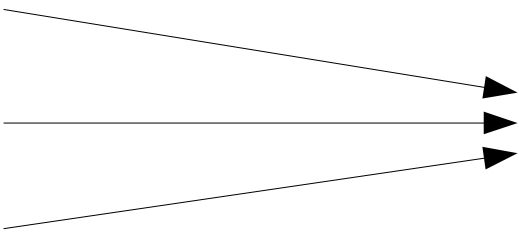
The diagram illustrates the process of renaming registers to a canonical form. On the left, three instructions are listed: `mov r1, r0`, `mov r4, r2`, and `mov r2, r8`. Three arrows originate from the right side of these instructions and point towards a single instruction on the right: `mov r1, r0`. This indicates that the original instructions are being mapped to a single canonical form where the registers are renamed to appear in sequence.

Canonical form

`mov r1, r0` has many equivalent versions

Rename each register so they appear in sequence:

`mov r1, r0`
`mov r4, r2`
`mov r2, r8`



`mov r1, r0`

With 16 registers this replaces 16×15 equivalent versions

Canonical form

```
add r4, r8, r1      add r2, r1, r0
orr r8, r4, #1      orr r1, r2, #1
sub r1, r2, #8      sub r0, r3, #8
```

Canonical form

```
add r4, r8, r1  
orr r8, r4, #1  
sub r1, r2, #8
```

→

```
add r2, r1, r0  
orr r1, r2, #1  
sub r0, r3, #8
```

Single three operand
instruction:

```
add rX, rX, rX
```

5 unique forms

→

```
add r0, r0, r0  
add r0, r0, r1  
add r0, r1, r0  
add r0, r1, r1  
add r0, r1, r2
```

Canonical form – reduction

Canonical form – reduction

Data processing instructions

- 16 ops, each using 3 of 16 possible registers.
- E.g. `add r0, r1, r2`
`sub r3, r4, r5`

Canonical form – reduction

Data processing instructions

- 16 ops, each using 3 of 16 possible registers.
- E.g. `add r0, r1, r2`
`sub r3, r4, r5`

Instructions	Normal	Canonical	Canonical (4 registers)
1	65,536	80	80
2	4,294,967,296	51,968	47,872
3	281,474,976,710,656	4,157,669,376	45,264,896
4	18,446,744,073,709,551,616	276,142,292,992	45,880,115,200

Canonical form – reduction

Data processing instructions

- 16 ops, each using 3 of 16 possible registers.
- E.g. `add r0, r1, r2`
`sub r3, r4, r5`

Instructions	Normal	Canonical	Canonical (4 registers)
1	65,536	80	80
2	4,294,967,296	51,968	47,872
3	281,474,976,710,656	4,157,669,376	45,264,896
4	18,446,744,073,709,551,616	276,142,292,992	45,880,115,200

@200,000 tests/second 2.9 million years

Canonical form – reduction

Data processing instructions

- 16 ops, each using 3 of 16 possible registers.
- E.g. `add r0, r1, r2`
`sub r3, r4, r5`

Instructions	Normal	Canonical	Canonical (4 registers)
1	65,536	80	80
2	4,294,967,296	51,968	47,872
3	281,474,976,710,656	4,157,669,376	45,264,896
4	18,446,744,073,709,551,616	276,142,292,992	45,880,115,200

@200,000 tests/second

2.9 million years

16 days


Canonical form – reduction

Data processing instructions

- 16 ops, each using 3 of 16 possible registers.
- E.g. `add r0, r1, r2`
`sub r3, r4, r5`

Instructions	Normal	Canonical	Canonical (4 registers)
1	65,536	80	80
2	4,294,967,296	51,968	47,872
3	281,474,976,710,656	4,157,669,376	45,264,896
4	18,446,744,073,709,551,616	276,142,292,992	45,880,115,200

@200,000 tests/second 2.9 million years 16 days <3 days



Instruction costing

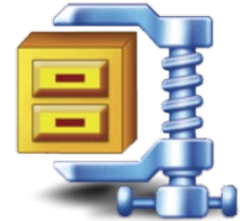
Instruction costing

Sequence cost is simple if code size is to be minimised



Instruction costing

Sequence cost is simple if code size is to be minimised



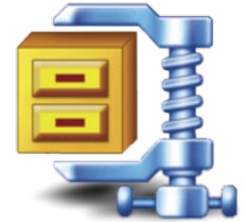
Difficult to accurately measure the performance of short sequences of instructions.

- Pipeline modelling
- Cycle accurate simulation



Instruction costing

Sequence cost is simple if code size is to be minimised



Difficult to accurately measure the performance of short sequences of instructions.

- Pipeline modelling
- Cycle accurate simulation



Energy

- Total Software Energy and Reporting (TSERO)



Instruction sets

Instruction sets

Characteristics of the instruction set affect how well a superoptimizer will perform.

Instruction sets

Characteristics of the instruction set affect how well a superoptimizer will perform.

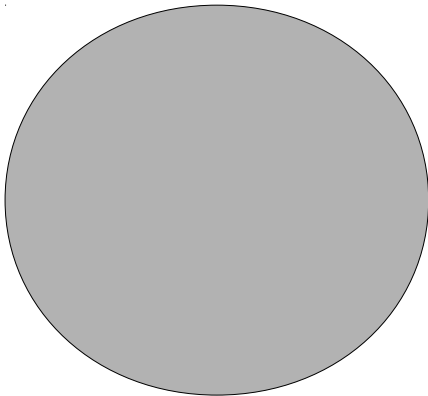
Smaller instruction set → fewer optimal sequences (?)

Instruction sets

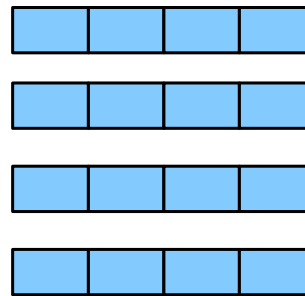
Characteristics of the instruction set affect how well a superoptimizer will perform.

Smaller instruction set → fewer optimal sequences (?)

Large instruction set



Many short sequences

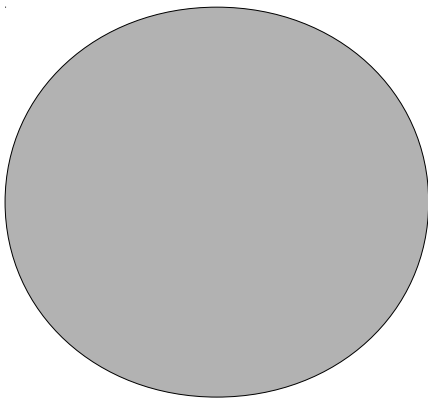


Instruction sets

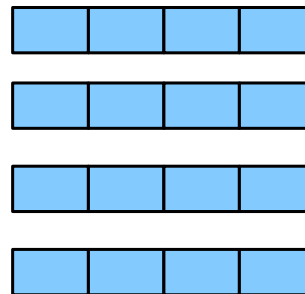
Characteristics of the instruction set affect how well a superoptimizer will perform.

Smaller instruction set → fewer optimal sequences (?)

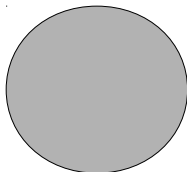
Large instruction set



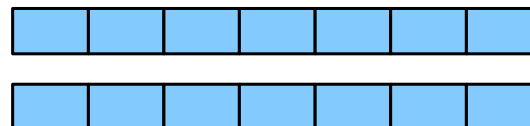
Many short sequences



Small instruction set



Few longer sequences

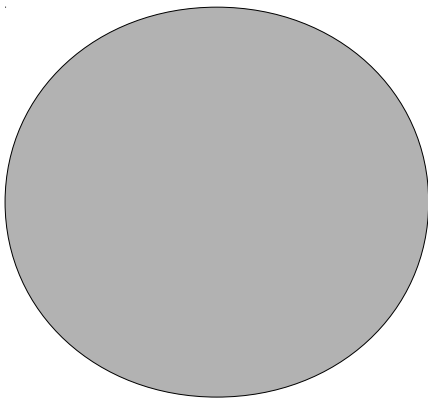


Instruction sets

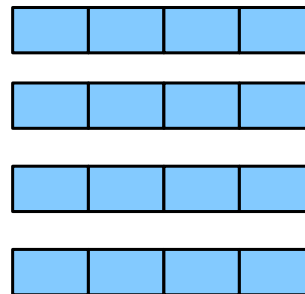
Characteristics of the instruction set affect how well a superoptimizer will perform.

Smaller instruction set → fewer optimal sequences (?)

Large instruction set

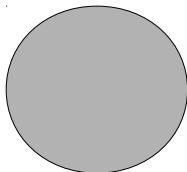


Many short sequences

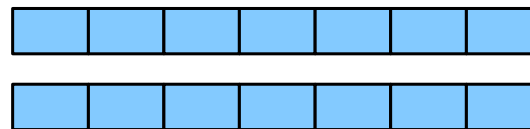


Hard for standard compilers

Small instruction set



Few longer sequences

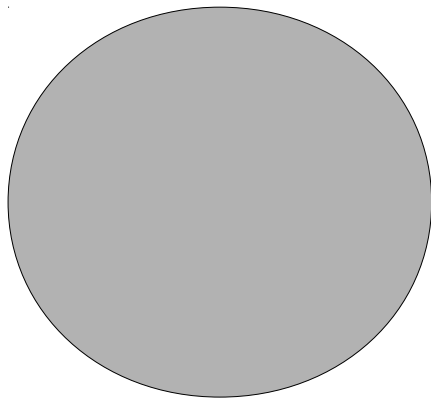


Instruction sets

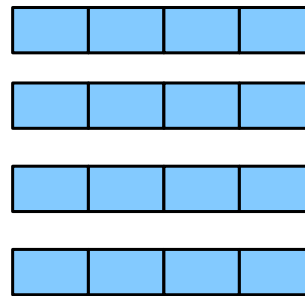
Characteristics of the instruction set affect how well a superoptimizer will perform.

Smaller instruction set → fewer optimal sequences (?)

Large instruction set

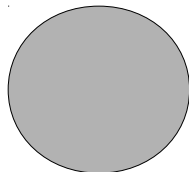


Many short sequences

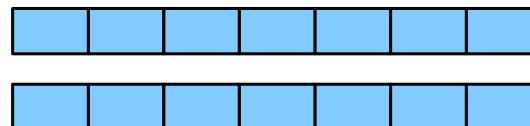


Hard for standard compilers

Small instruction set



Few longer sequences



Easier for standard compilers

Superoptimizers

Superoptimizers

GNU SuperOptimizer (GSO)

Superoptimizers

GNU SuperOptimizer (GSO)

Denali

Superoptimizers

GNU SuperOptimizer (GSO)

Denali

Peephole Superoptimizer

Superoptimizers

GNU SuperOptimizer (GSO)

Denali

Peephole Superoptimizer

Stochastic Superoptimization

Superoptimizers

GNU SuperOptimizer (GSO)

Denali

Peephole Superoptimizer

Stochastic Superoptimization

Other

- A Hacker's Assistant (similar to GSO)
- TOAST (similar to Denali)

GNU SuperOptimizer

Focuses on elimination of short basic blocks

Granlund, T., & Kenner, R. (1992). Eliminating branches using a superoptimizer and the GNU C compiler. PLDI '92 Proceedings of the ACM SIGPLAN 1992 conference on Programming language design and implementation.

GNU SuperOptimizer

Focuses on elimination of short basic blocks

```
unsigned a, b, c;
```

```
if (a < b)  
    c++;
```



```
    cmp     eax, ebx  
    jge    L1  
    add    ecx, #1  
L1:  
    ...
```

Granlund, T., & Kenner, R. (1992). Eliminating branches using a superoptimizer and the GNU C compiler. PLDI '92 Proceedings of the ACM SIGPLAN 1992 conference on Programming language design and implementation.

GNU SuperOptimizer

Focuses on elimination of short basic blocks

```
unsigned a, b, c;
```

```
if (a < b)  
    c++;
```



```
    cmp     eax, ebx  
    jge    L1  
    add    ecx, #1  
L1:  
    ...
```

```
c = (a < b) + c;
```



```
    subl   eax, edx  
    adcl   ecx, #0
```

Granlund, T., & Kenner, R. (1992). Eliminating branches using a superoptimizer and the GNU C compiler. PLDI '92 Proceedings of the ACM SIGPLAN 1992 conference on Programming language design and implementation.

Denali

5	3			7			
6			1	9	5		
	9	8					6
8							3
4							1
$0x = 0$	$xx = x$	$x\bar{x} = 0$	$xy = yx$	$(xy)z = x(yz)$	$x+y+z = (x+y)(x+z)$	$x(x+y) = x$	$1+x = 1$
$x+x = x$	$x+\bar{x} = 1$	$x+y = y+x$	$x(y+z) = xy+xz$	$x(y+z) = xy+xz$	$x+xy = x$		

Joshi, R., Nelson, G., & Randall, K. (2001). Denali : a goal-directed superoptimizer. Proceedings of the ACM 2000 Conference on Programming Language Design and Implementation (pp. 304–314).

Denali

Rule based program generation:

5	3			7			
6			1	9	5		
	9	8					6
8							3
4							1
							6
							5
							8
							7
							9

$0x = 0$

$xx = x$

$x\bar{x} = 0$

$xy = yx$

$(xy)z = x(yz)$

$x+yz = (x+y)(x+z)$

$x(x+y) = x$

$1+x = 1$

$x+x = x$

$x+\bar{x} = 1$

$x+y = y+x$

$(x+y)+z = x+(y+z)$

$x(y+z) = xy+xz$

$x+xy = x$

Joshi, R., Nelson, G., & Randall, K. (2001). Denali : a goal-directed superoptimizer. Proceedings of the ACM 2000 Conference on Programming Language Design and Implementation (pp. 304–314).

Denali

Rule based program generation:

- Prove the condition: there exists no instruction sequence that solves $F(x)$ in $< K$ cycles

5	3			7			
6			1	9	5		
	9	8					6
8							3
4							1
$0x = 0$	$xx = x$	$x\bar{x} = 0$	$xy = yx$	$(xy)z = x(yz)$	$x+y+z = (x+y)(x+z)$	$x(x+y) = x$	
$1+x = 1$	$x+x = x$	$x+\bar{x} = 1$	$x+y = y+x$	$(x+y)+z = x+(y+z)$	$x(y+z) = xy+xz$	$x+xy = x$	
							5
							8
							7
							9

Joshi, R., Nelson, G., & Randall, K. (2001). Denali : a goal-directed superoptimizer. Proceedings of the ACM 2000 Conference on Programming Language Design and Implementation (pp. 304–314).

Denali

Rule based program generation:

- Prove the condition: there exists no instruction sequence that solves $F(x)$ in $< K$ cycles
- Failure yields an example sequence

5	3			7			
6			1	9	5		
	9	8					6
8							3
4							1
							6
							5
							8
							7
							9

0x = 0
xx = x
x̄x = 0
xy = yx
(xy)z = x(yz)
x+y+z = (x+y)(x+z)
x(x+y) = x

1+x = 1
x+x = x
x+x̄ = 1
x+y = y+x
(x+y)+z = x+(y+z)
x(y+z) = xy+xz
x+xy = x

Joshi, R., Nelson, G., & Randall, K. (2001). Denali : a goal-directed superoptimizer. Proceedings of the ACM 2000 Conference on Programming Language Design and Implementation (pp. 304–314).

Denali

Rule based program generation:

- Prove the condition: there exists no instruction sequence that solves $F(x)$ in $< K$ cycles
- Failure yields an example sequence
- Use hand-written transformation rules

$$\begin{aligned} x * 2 &\leftrightarrow x \ll 1 \\ a + b &\leftrightarrow b + a \end{aligned}$$

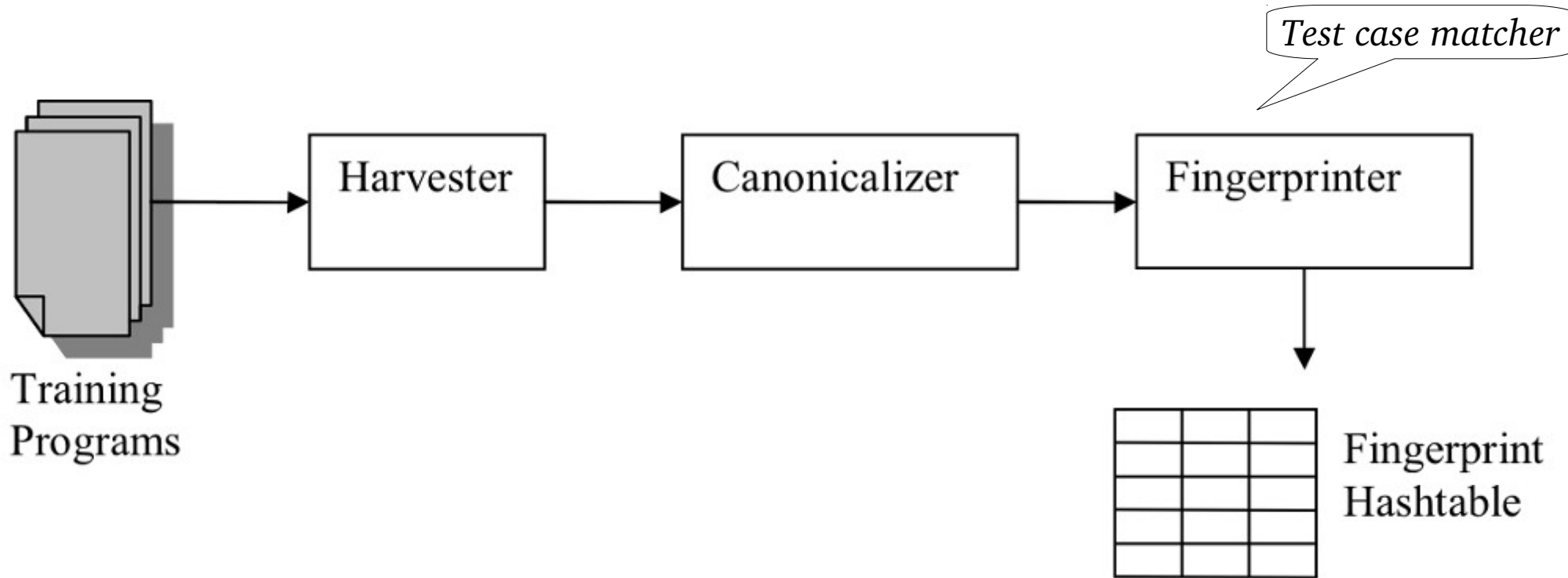
5	3			7			
6			1	9	5		
	9	8					6
8							3
4							1
							6
							5
			8			7	9

$$\begin{aligned} 0x &= 0 & 1+x &= 1 \\ xx &= x & x+x &= x \\ x\bar{x} &= 0 & x+\bar{x} &= 1 \\ xy &= yx & x+y &= y+x \\ (xy)z &= x(yz) & x+y+z &= x+(y+z) \\ x+y+z &= (x+y)(x+z) & x(y+z) &= xy+xz \\ x(x+y) &= x & x+xy &= x \end{aligned}$$

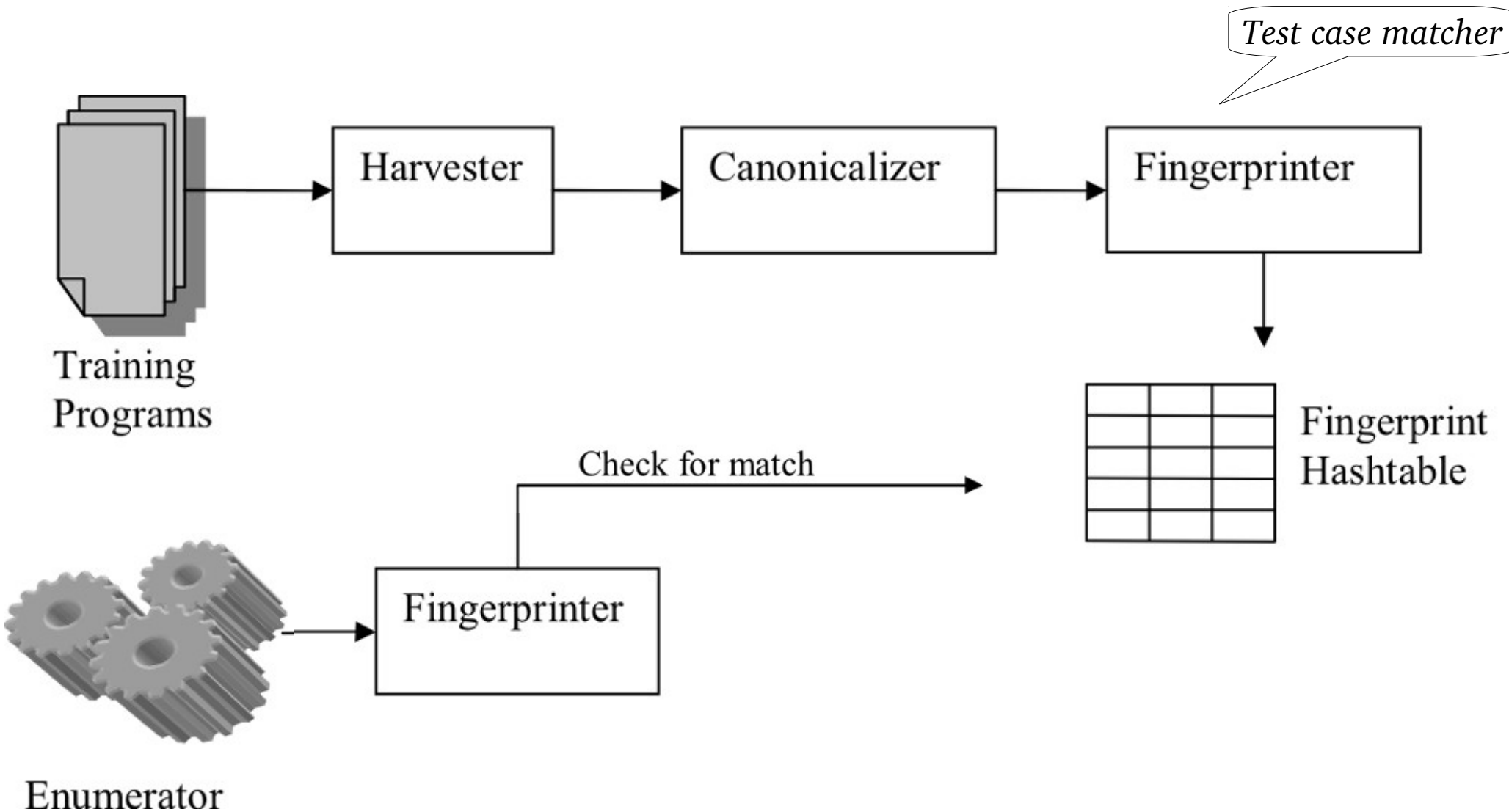
Joshi, R., Nelson, G., & Randall, K. (2001). Denali : a goal-directed superoptimizer. Proceedings of the ACM 2000 Conference on Programming Language Design and Implementation (pp. 304–314).

Peephole Superoptimizers

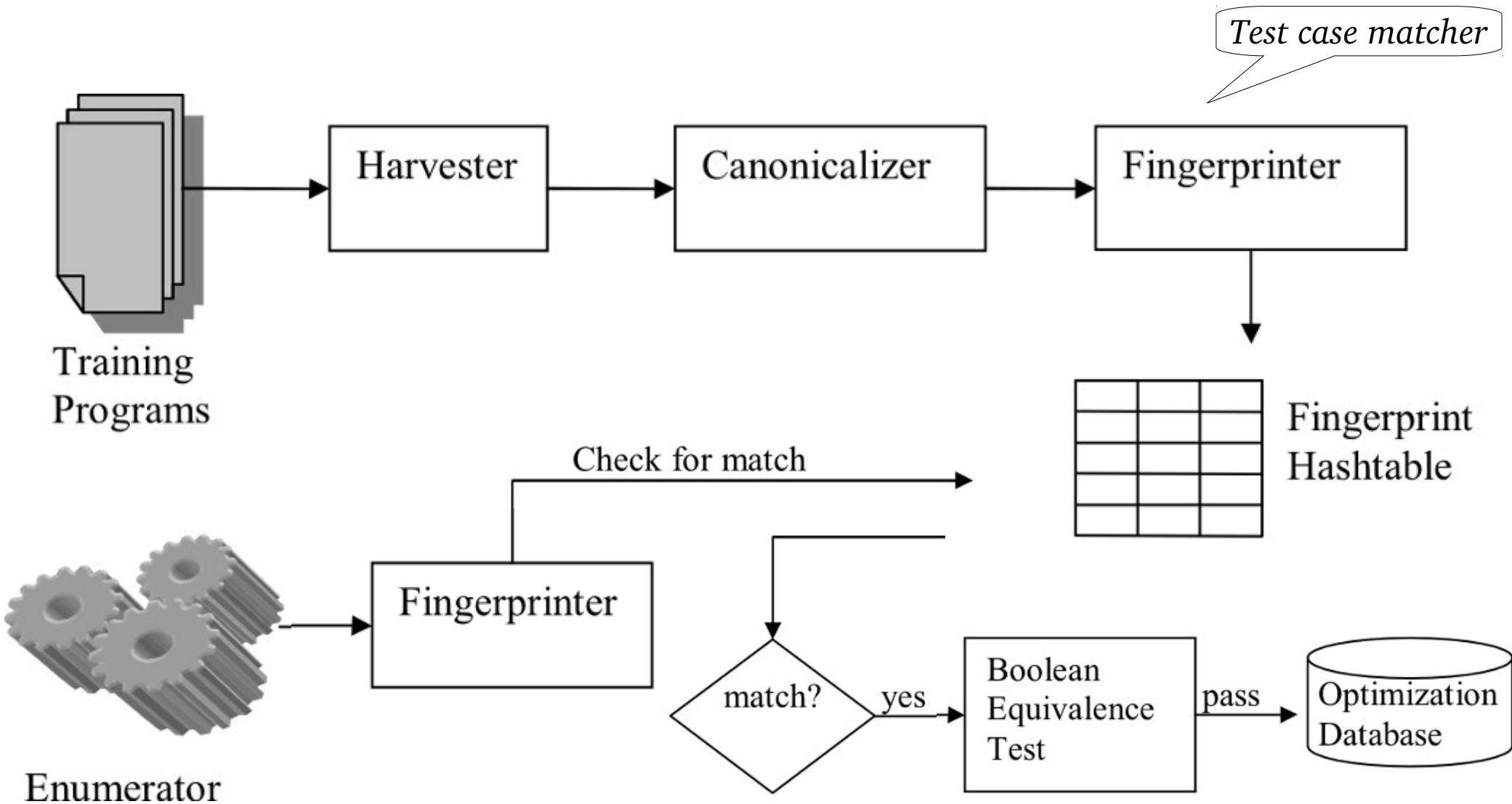
Peephole Superoptimizers



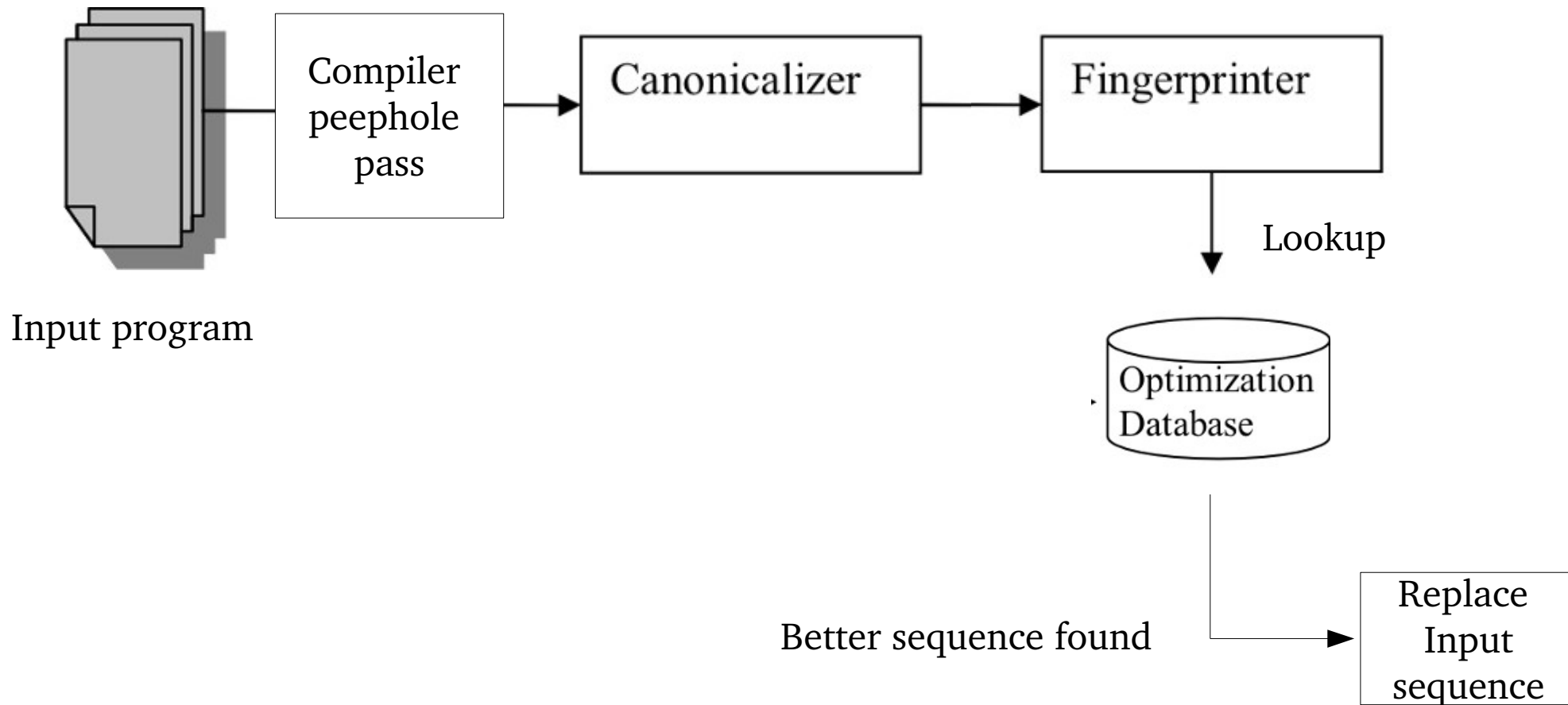
Peephole Superoptimizers



Peephole Superoptimizers



Peephole Superoptimizers



Stochastic superoptimization

Schkufza, E., Sharma, R., & Aiken, A. (2013). Stochastic superoptimization. Architectural Support for Programming Languages and Operating Systems, 305.

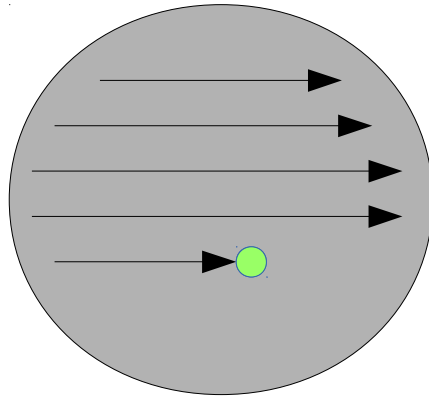
Stochastic superoptimization

A different approach to instruction sequence enumeration

Schkufza, E., Sharma, R., & Aiken, A. (2013). Stochastic superoptimization. Architectural Support for Programming Languages and Operating Systems, 305.

Stochastic superoptimization

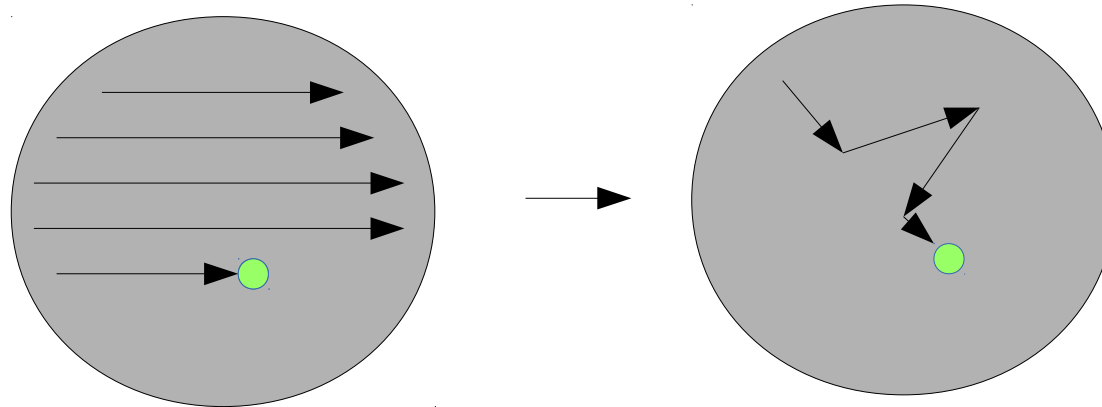
A different approach to instruction sequence enumeration



Schkufza, E., Sharma, R., & Aiken, A. (2013). Stochastic superoptimization. Architectural Support for Programming Languages and Operating Systems, 305.

Stochastic superoptimization

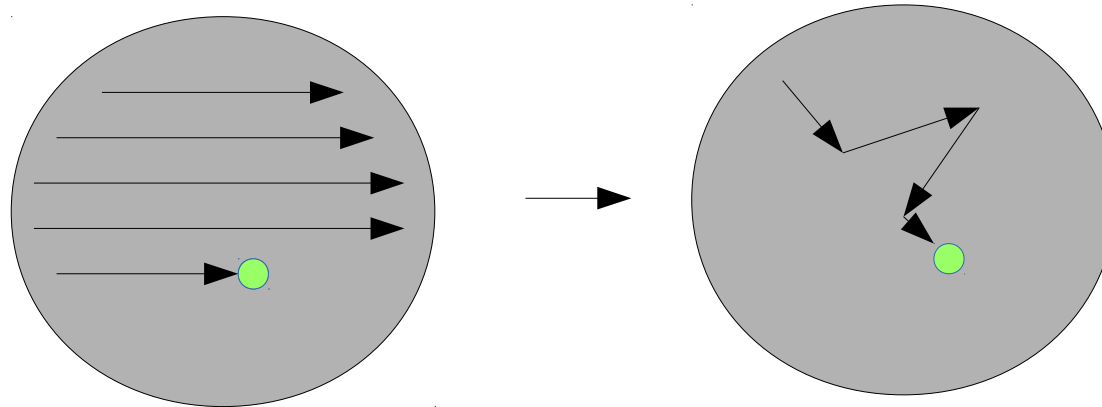
A different approach to instruction sequence enumeration



Schkufza, E., Sharma, R., & Aiken, A. (2013). Stochastic superoptimization. Architectural Support for Programming Languages and Operating Systems, 305.

Stochastic superoptimization

A different approach to instruction sequence enumeration



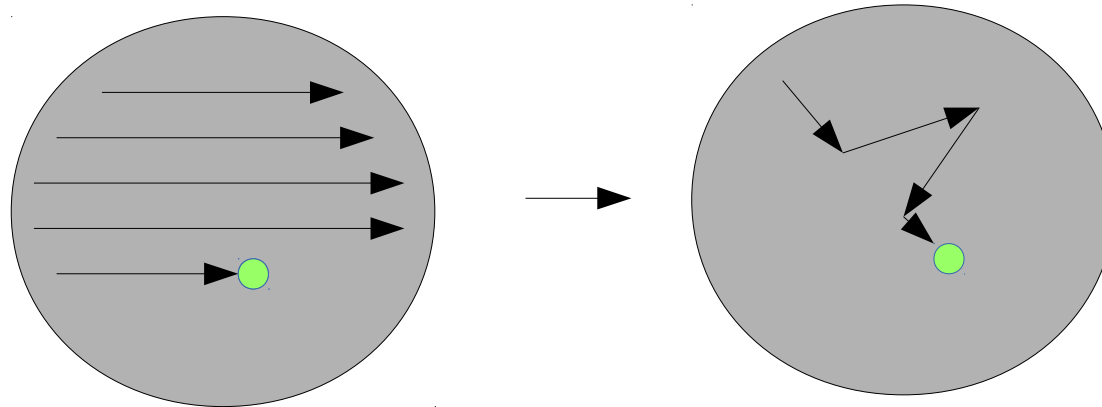
Longer sequences of instructions

- Sequences of > 14 instructions were considered

Schkufza, E., Sharma, R., & Aiken, A. (2013). Stochastic superoptimization. Architectural Support for Programming Languages and Operating Systems, 305.

Stochastic superoptimization

A different approach to instruction sequence enumeration



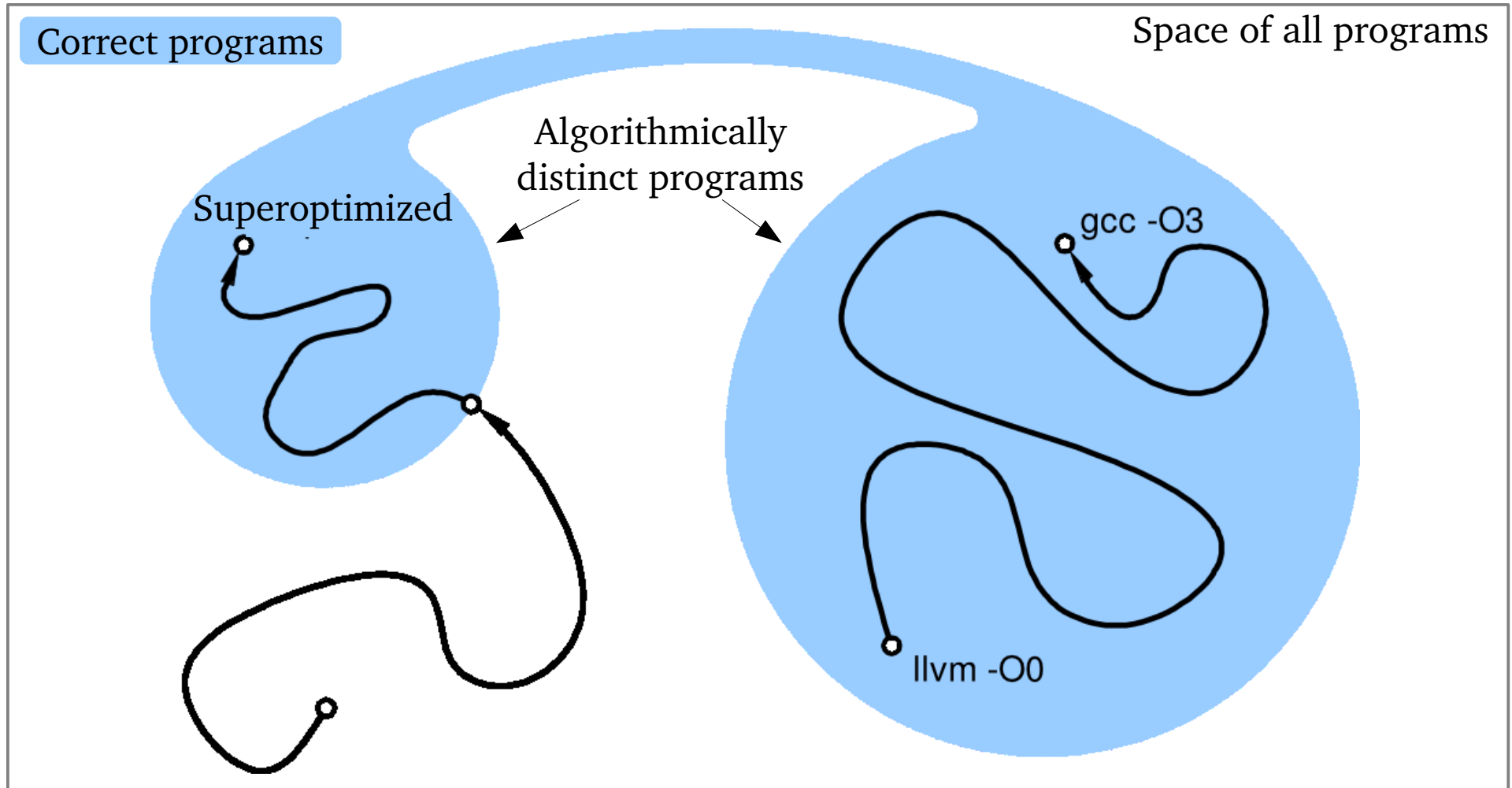
Longer sequences of instructions

- Sequences of > 14 instructions were considered
- E.g. OpenSSL Montgomery multiplication 60% faster

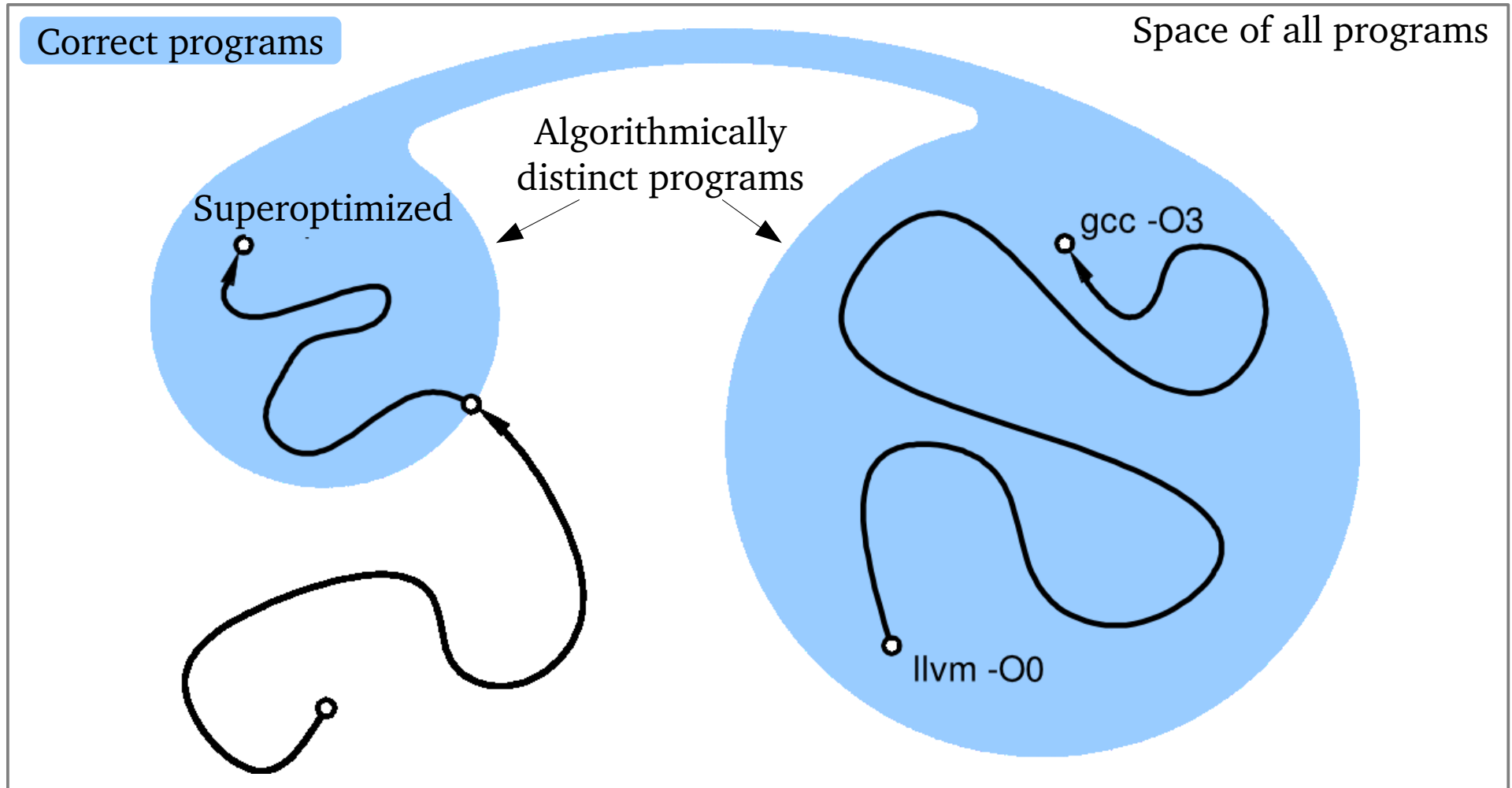
Schkufza, E., Sharma, R., & Aiken, A. (2013). Stochastic superoptimization. Architectural Support for Programming Languages and Operating Systems, 305.

Discovering new algorithms

Discovering new algorithms



Discovering new algorithms



Stochastic superoptimization's longer sequences make this more likely

Plan for today

What is superoptimization?



Latest developments

NEW

The GNU SuperOptimizer



GSO: What can it do?

The sign function, AVR:

```
cp    r1, r24
brlt  .+14
ldi   r25, 0x01
cpse  r24, r1
rjmp  .+2
ldi   r25, 0x00
mov   r24, r25
neg   r24
rjmp  .+2
ldi   r24, 0x01
```

Compiler (-Os)

11 instructions

4-10 cycles (if r1 initialised to 0)

```
add  r0, r0
mov  r1, r0
sbc  r1, r0
sub  r1, r0
adc  r1, r0
```

Superoptimizer:

5 instructions

5 cycles

How does it work?

Iterative deepening depth first search

1 instruction

How does it work?

Iterative deepening depth first search

1 instruction

add r0, r0 → Check

How does it work?

Iterative deepening depth first search

1 instruction

add r0, r0 → Check

sub r0, r0 → Check

How does it work?

Iterative deepening depth first search

1 instruction

add r0, r0 → Check

sub r0, r0 → Check

mul r0, r0 → Check

How does it work?

Iterative deepening depth first search

2 instructions

How does it work?

Iterative deepening depth first search

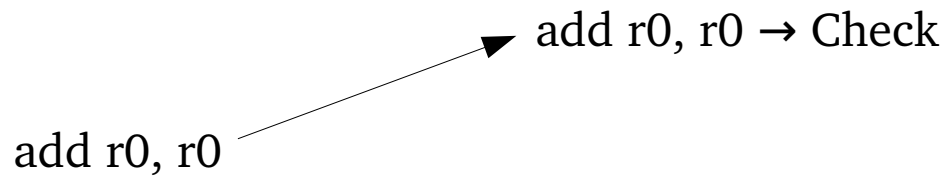
2 instructions

```
add r0, r0
```

How does it work?

Iterative deepening depth first search

2 instructions

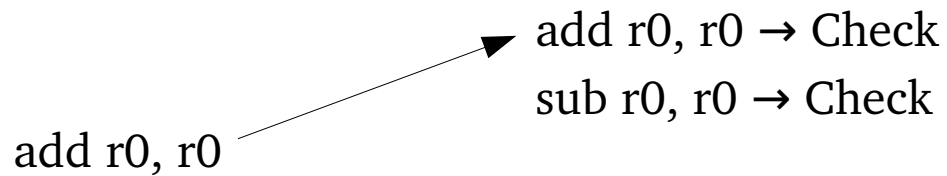


How does it work?

Iterative deepening depth first search

2 instructions

add r0, r0 → Check
sub r0, r0 → Check

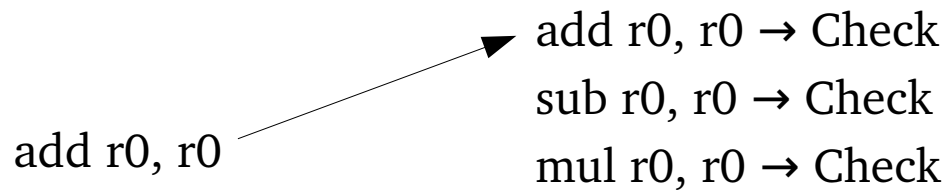
A diagram illustrating the execution of two instructions. On the left, the instruction 'add r0, r0' is written. An arrow points from this instruction to the right, where two lines of text are listed: 'add r0, r0 → Check' and 'sub r0, r0 → Check'. This indicates that the 'add' instruction is being checked against both possible instructions.

How does it work?

Iterative deepening depth first search

2 instructions

add r0, r0 → Check
sub r0, r0 → Check
mul r0, r0 → Check

A diagram illustrating the execution of instructions. On the left, the text 'add r0, r0' is followed by a thin black arrow pointing to the right. The arrow points to a list of three instructions: 'add r0, r0 → Check', 'sub r0, r0 → Check', and 'mul r0, r0 → Check'. Each instruction is on a new line and ends with '→ Check'.

How does it work?

Iterative deepening depth first search

2 instructions

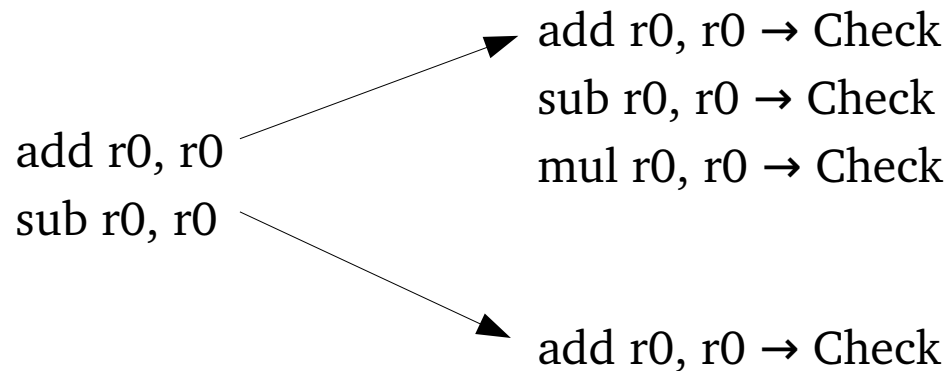
add r0, r0
sub r0, r0

→ add r0, r0 → Check
sub r0, r0 → Check
mul r0, r0 → Check

How does it work?

Iterative deepening depth first search

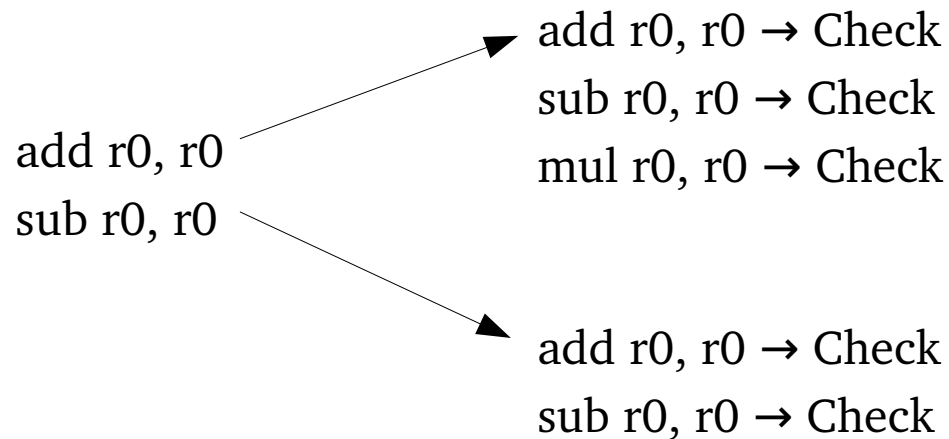
2 instructions



How does it work?

Iterative deepening depth first search

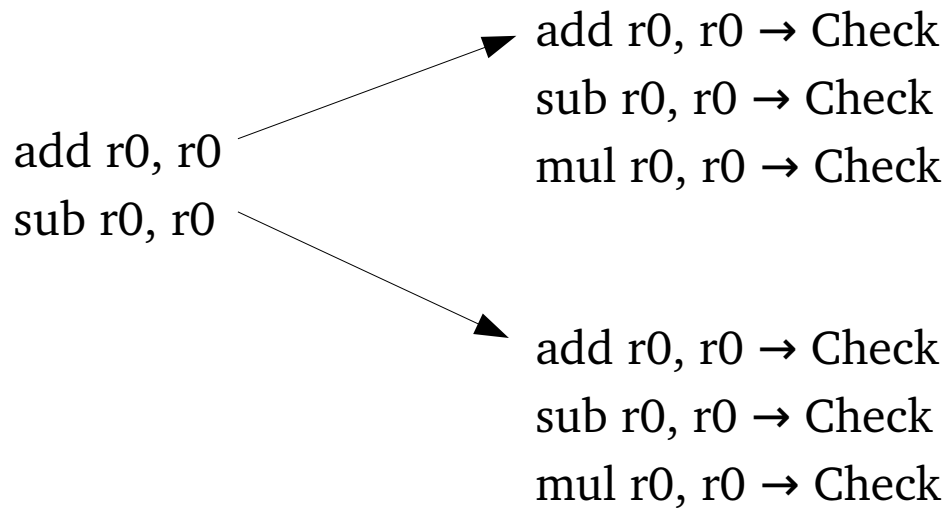
2 instructions



How does it work?

Iterative deepening depth first search

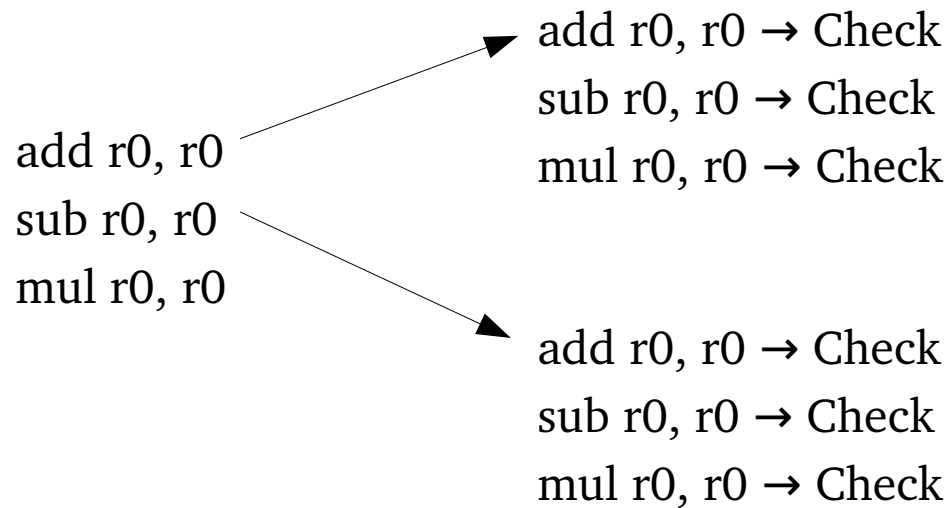
2 instructions



How does it work?

Iterative deepening depth first search

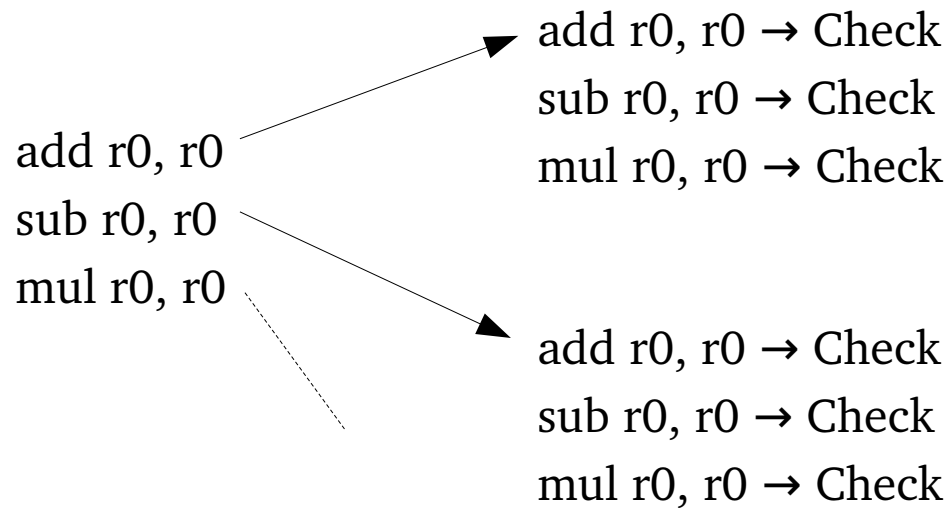
2 instructions



How does it work?

Iterative deepening depth first search

2 instructions



...

How does it work?

Iterative deepening depth first search

3 instructions

How does it work?

Iterative deepening depth first search

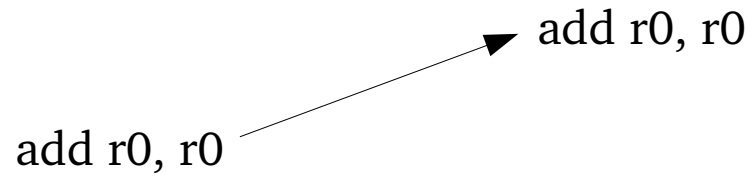
3 instructions

```
add r0, r0
```

How does it work?

Iterative deepening depth first search

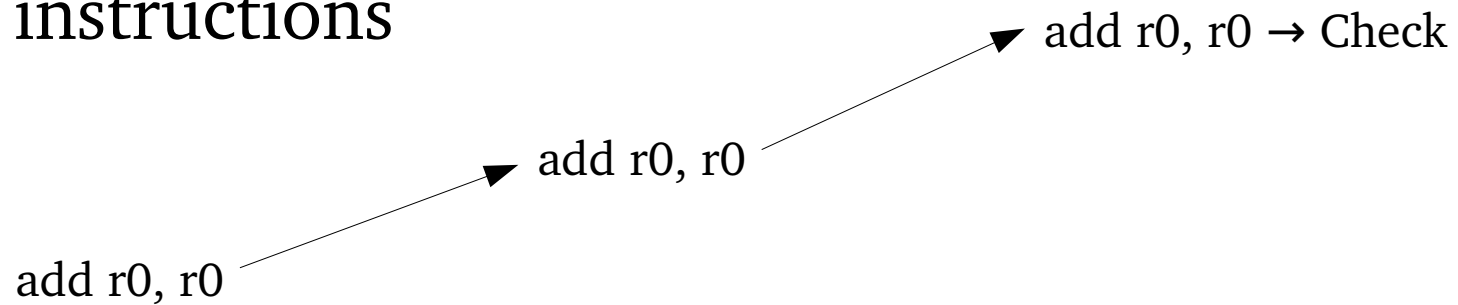
3 instructions



How does it work?

Iterative deepening depth first search

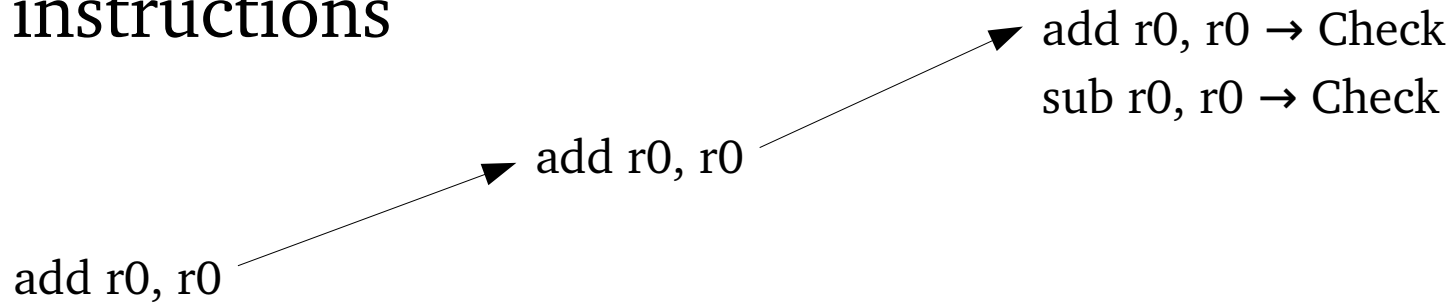
3 instructions



How does it work?

Iterative deepening depth first search

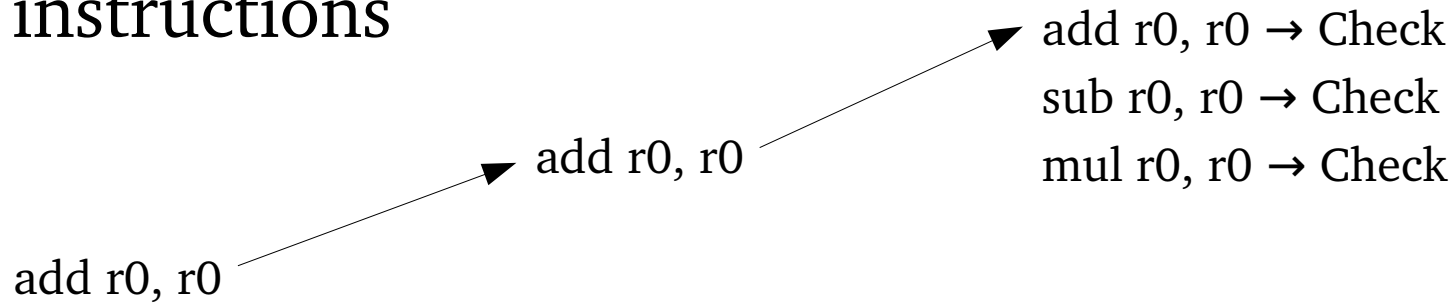
3 instructions



How does it work?

Iterative deepening depth first search

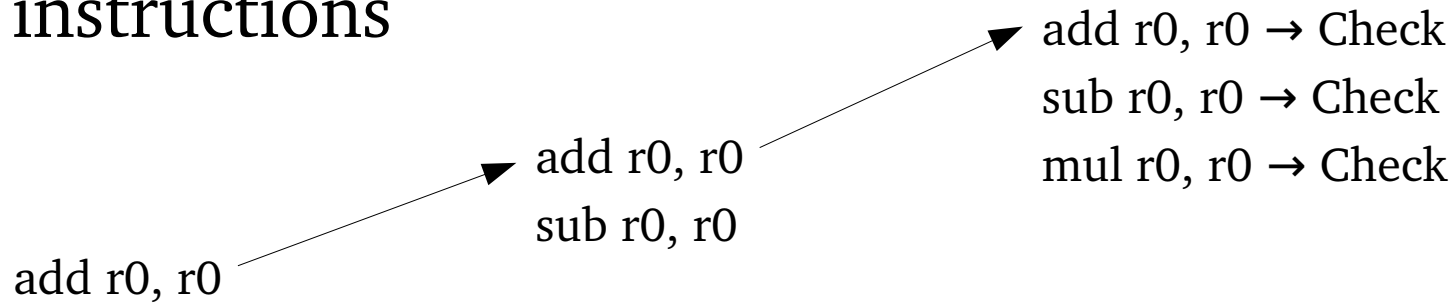
3 instructions



How does it work?

Iterative deepening depth first search

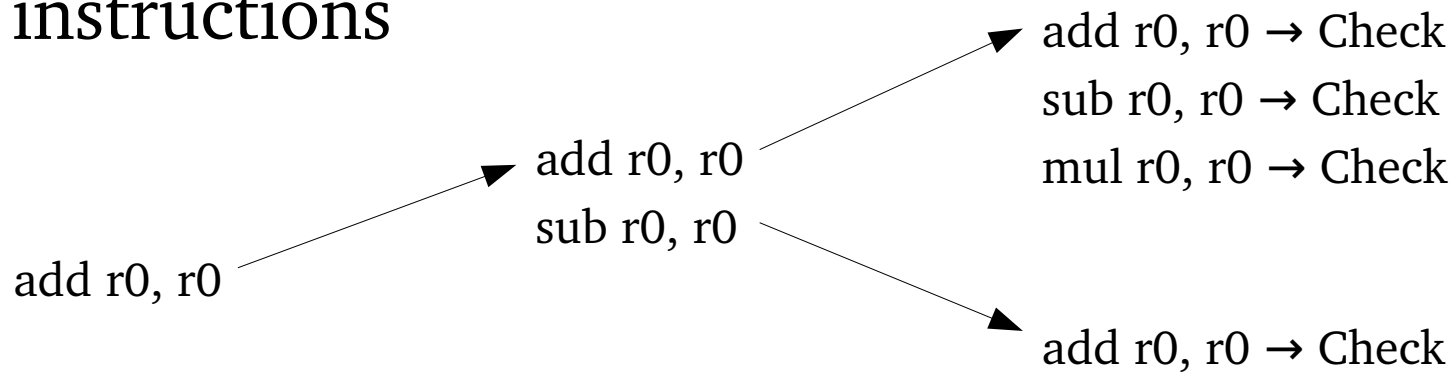
3 instructions



How does it work?

Iterative deepening depth first search

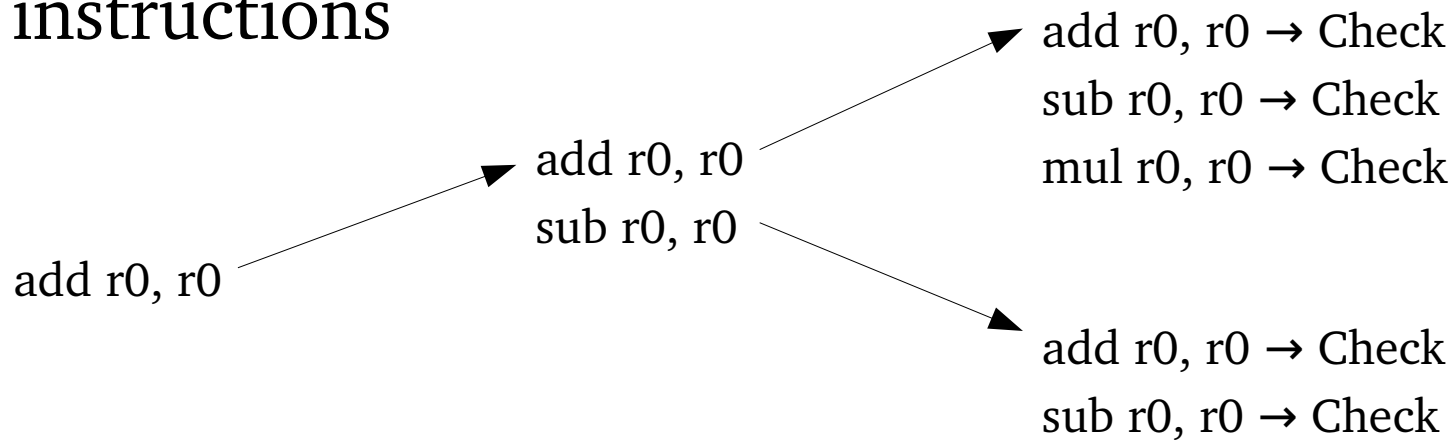
3 instructions



How does it work?

Iterative deepening depth first search

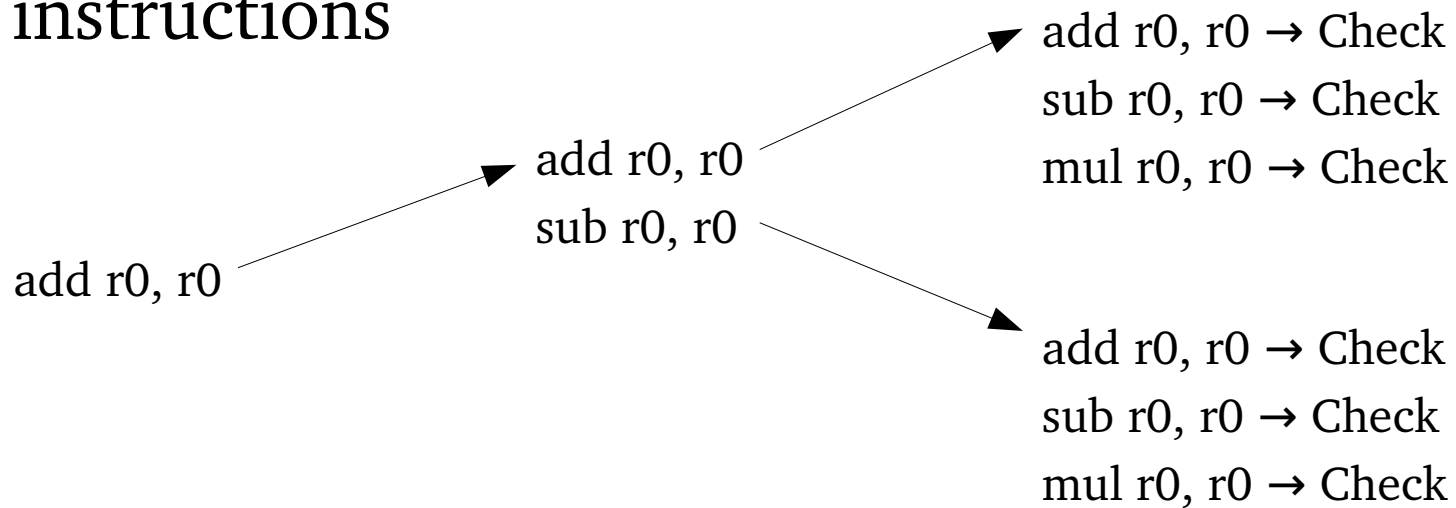
3 instructions



How does it work?

Iterative deepening depth first search

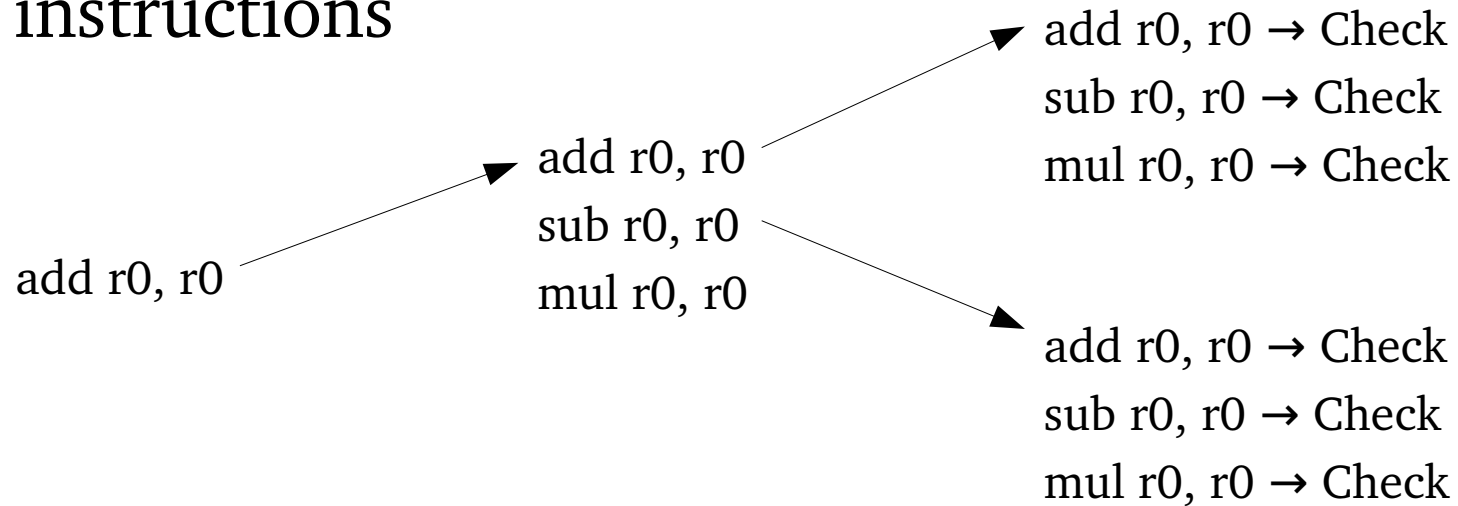
3 instructions



How does it work?

Iterative deepening depth first search

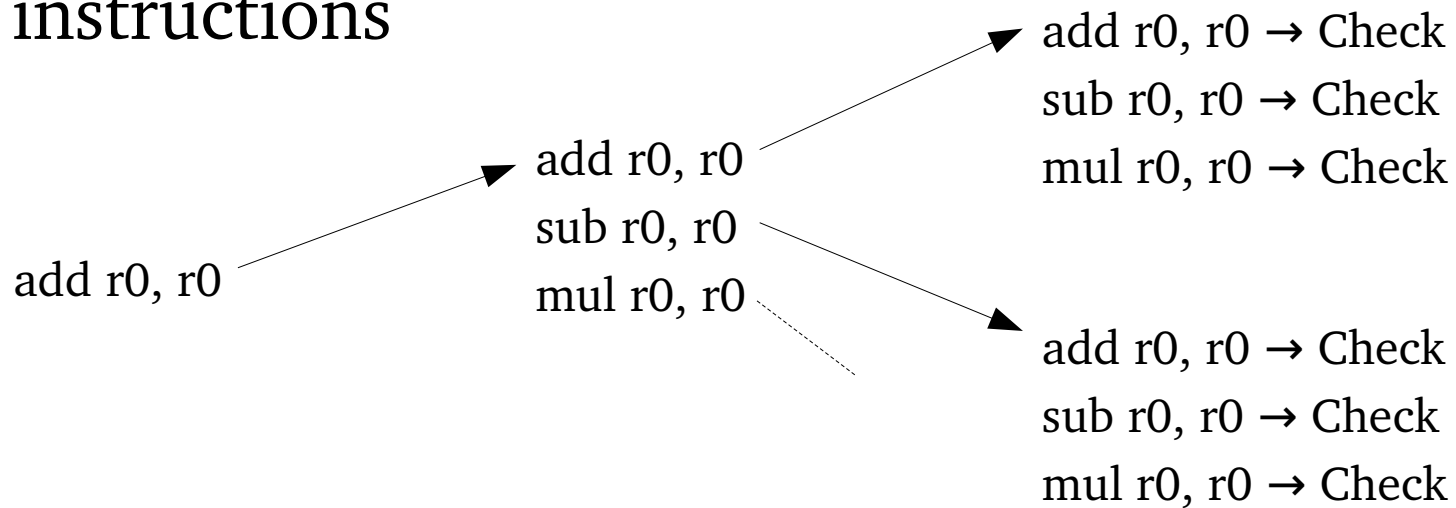
3 instructions



How does it work?

Iterative deepening depth first search

3 instructions

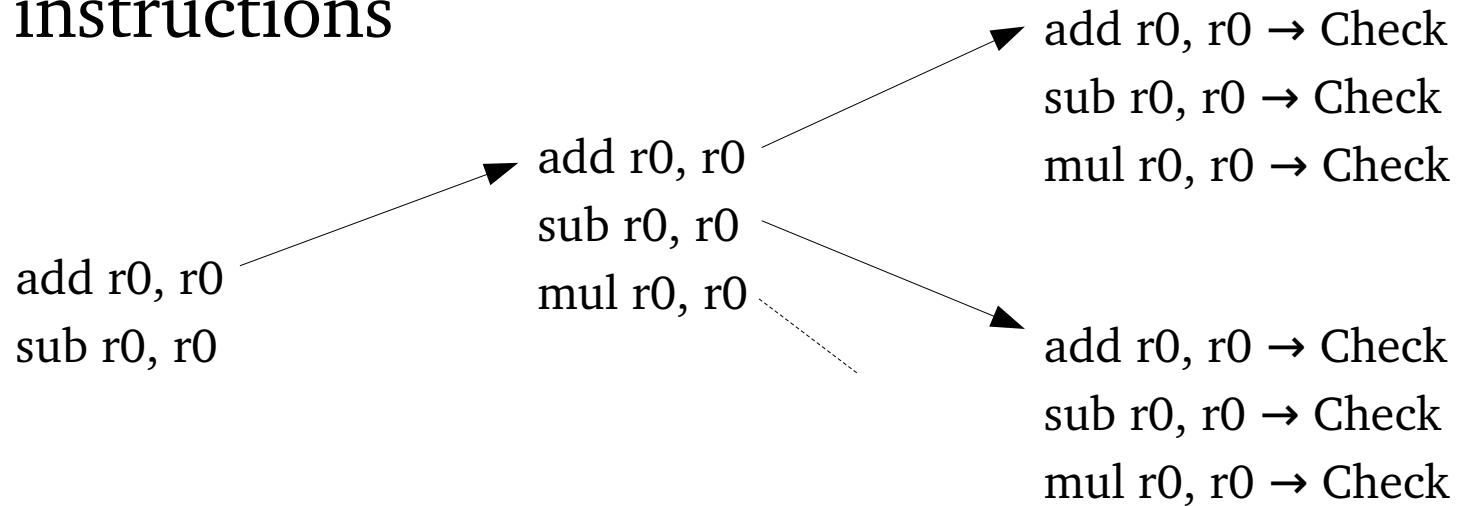


...

How does it work?

Iterative deepening depth first search

3 instructions

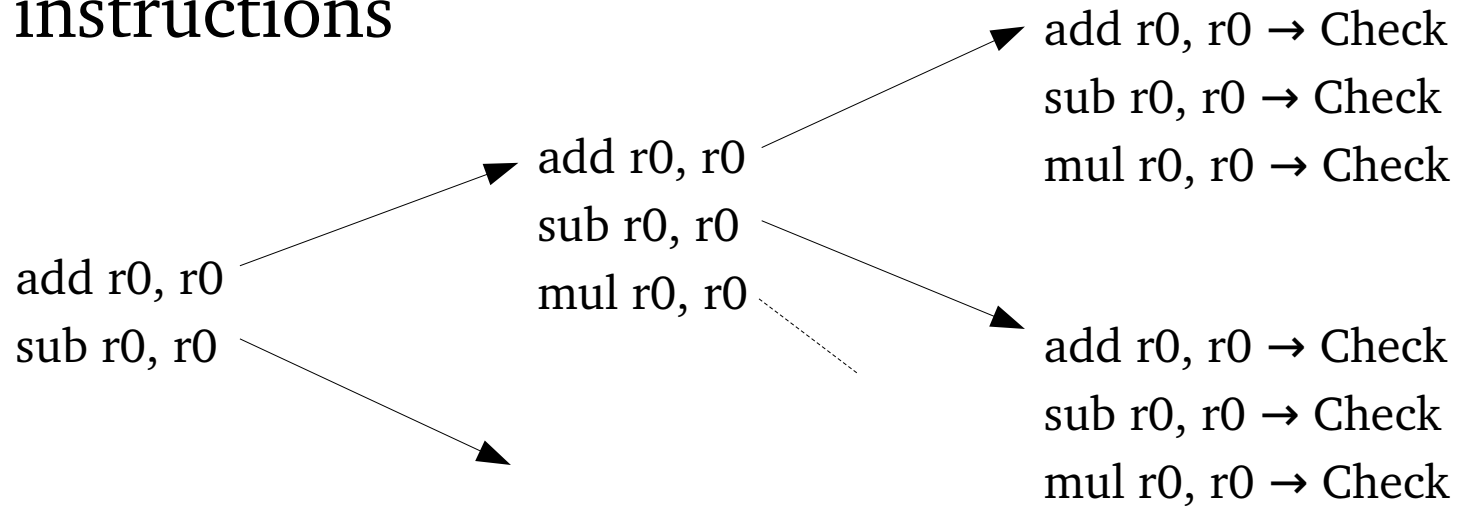


...

How does it work?

Iterative deepening depth first search

3 instructions

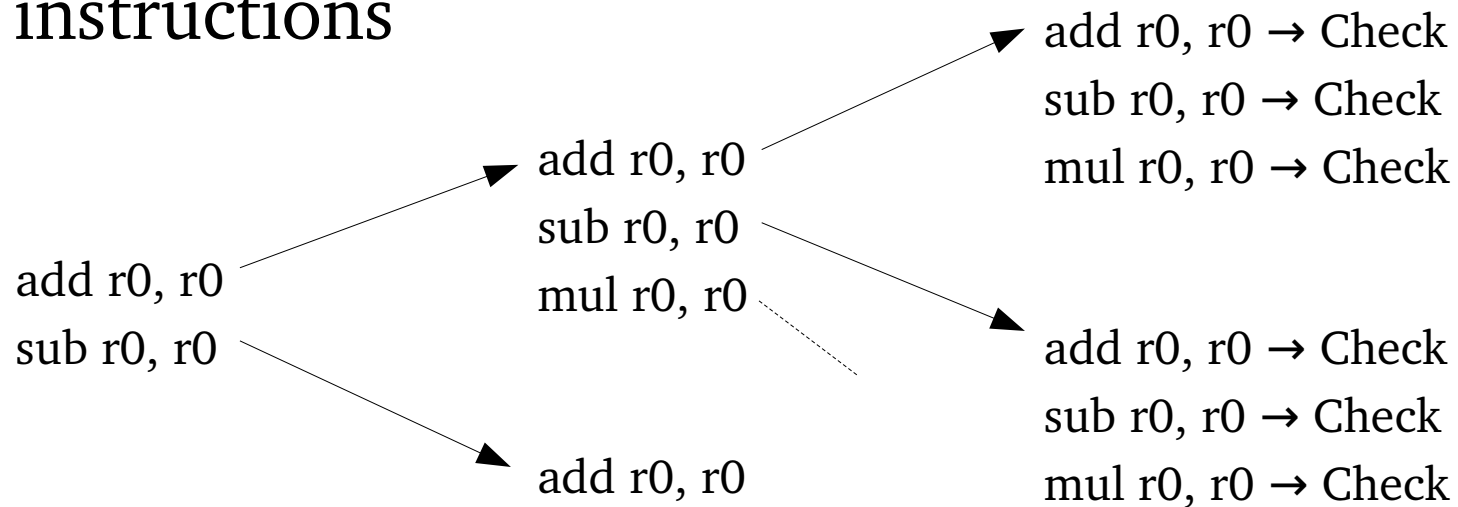


...

How does it work?

Iterative deepening depth first search

3 instructions

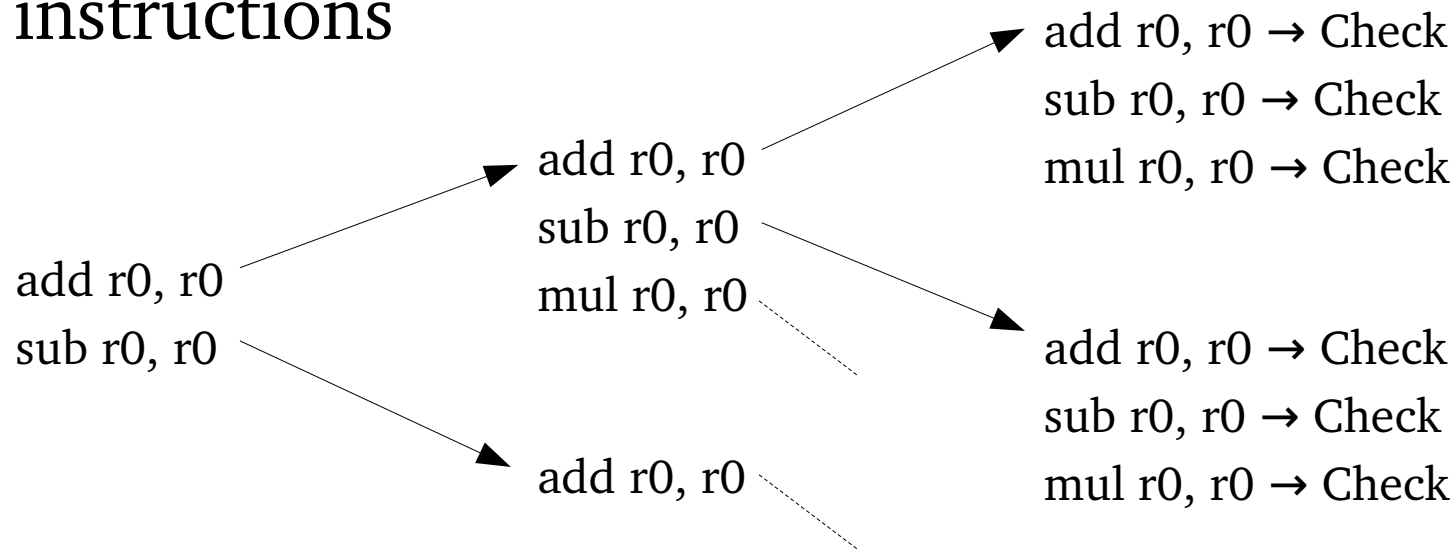


...

How does it work?

Iterative deepening depth first search

3 instructions

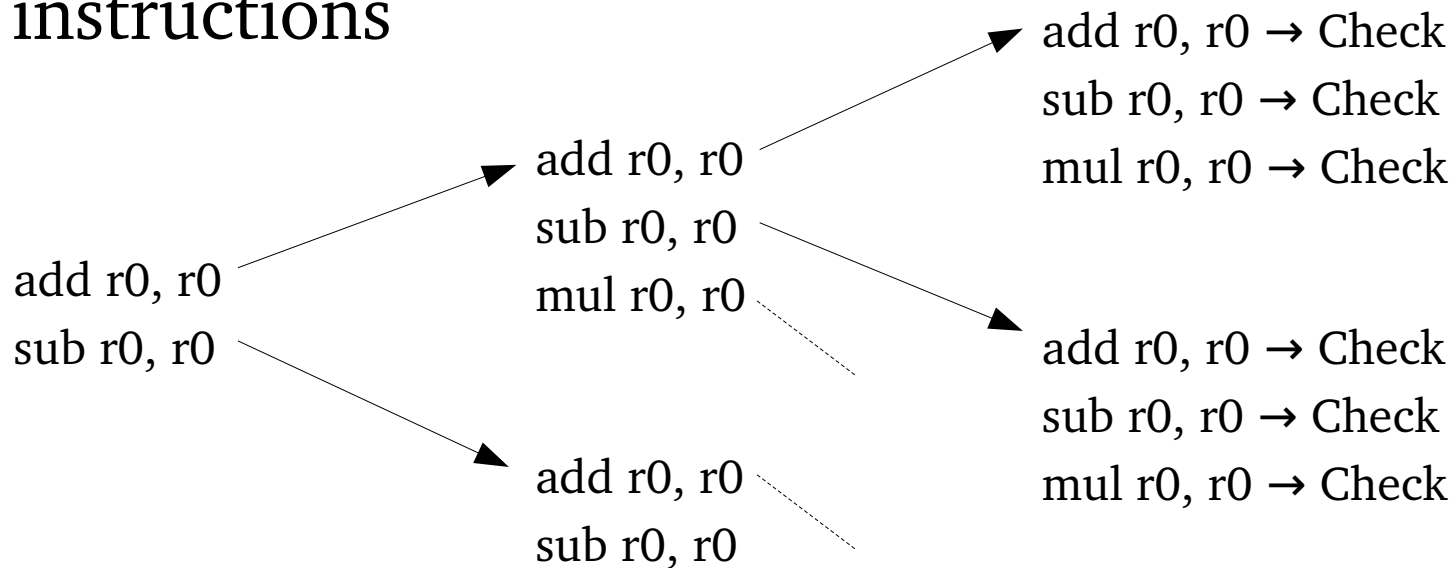


...

How does it work?

Iterative deepening depth first search

3 instructions

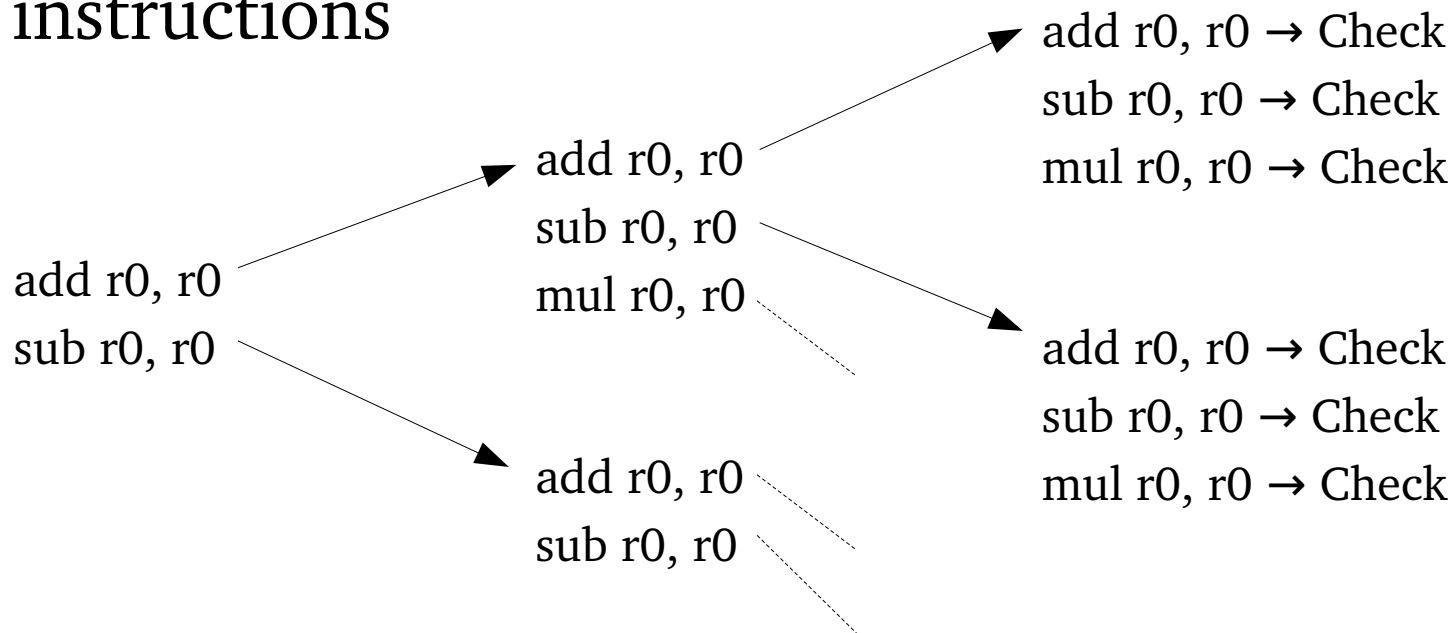


...

How does it work?

Iterative deepening depth first search

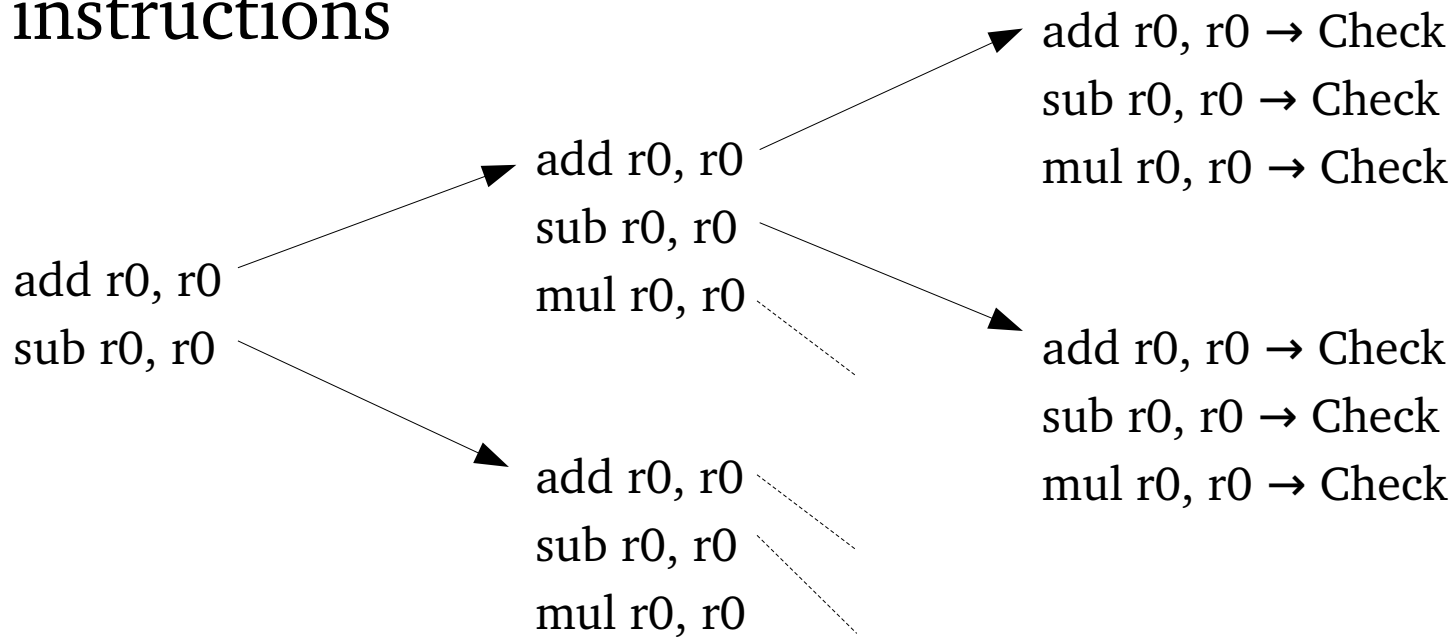
3 instructions



How does it work?

Iterative deepening depth first search

3 instructions

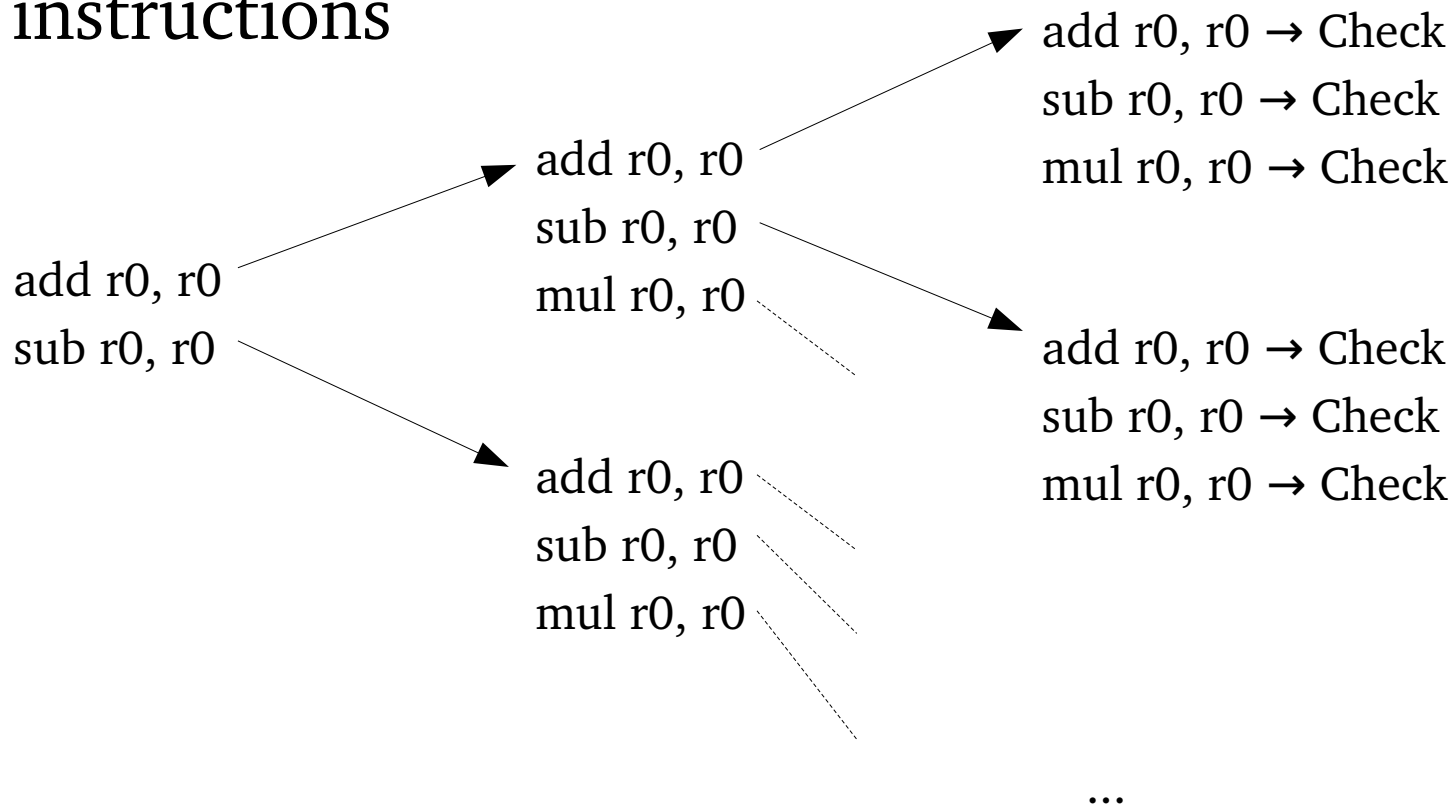


...

How does it work?

Iterative deepening depth first search

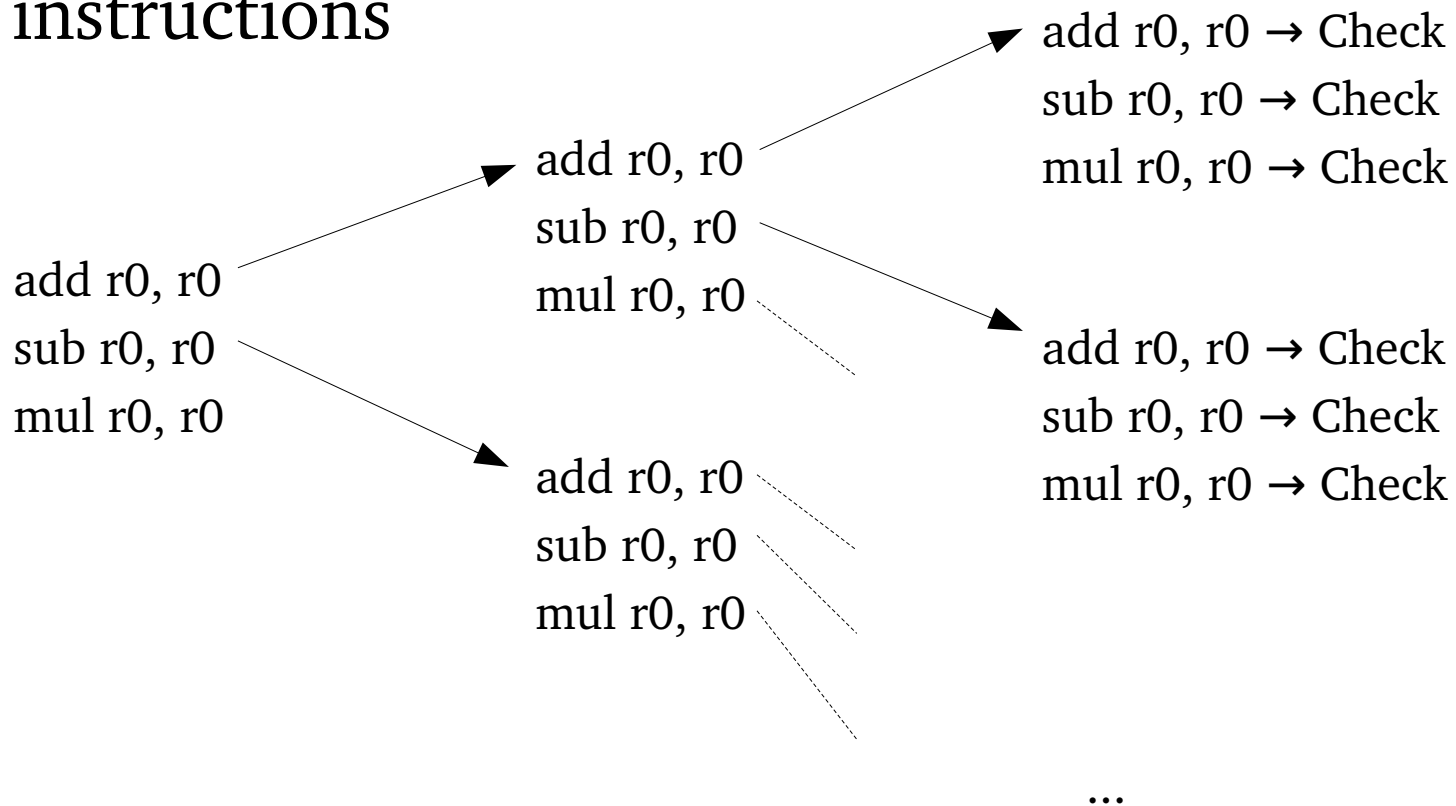
3 instructions



How does it work?

Iterative deepening depth first search

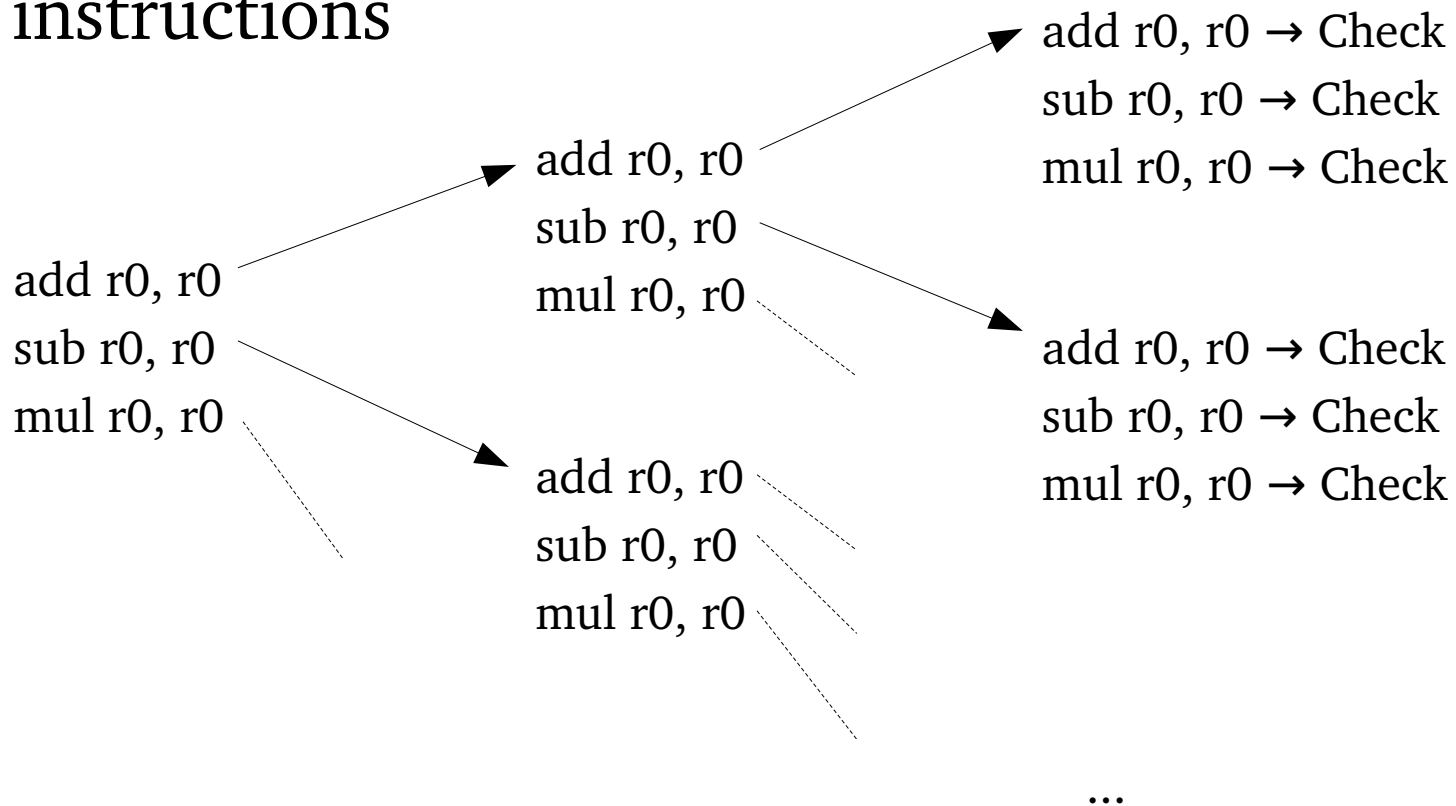
3 instructions



How does it work?

Iterative deepening depth first search

3 instructions



How to add a new goal

How to add a new goal

Goal is GSO's term for a target function to superoptimize

How to add a new goal

Goal is GSO's term for a target function to superoptimize

File: `goal.def`

How to add a new goal

Goal is GSO's term for a target function to superoptimize

File: goal.def

Examples:

```
DEF_GOAL (SHIFTL_1, 1, "s111", { r = v0 << 1; })
```

```
DEF_GOAL (SHIFTL_2, 1, "s112", { r = v0 << 2; })
```

How to add a new goal

Goal is GSO's term for a target function to superoptimize

File: goal.def

Examples:

```
DEF_GOAL (SHIFTL_1, 1, "sll1", { r = v0 << 1; })
DEF_GOAL (SHIFTL_2, 1, "sll2", { r = v0 << 2; })
DEF_GOAL (SIGNUM, 1, "signum",
{
    if(v0 < 0)
        r = -1;
    else if(v0 > 0)
        r = 1;
    else
        r = 0;
})
```

How to add a new goal

How to add a new goal

```
DEF_GOAL (EQ_MINUS, 3, "eq-", { r = v2 - (v0 == v1); })
```

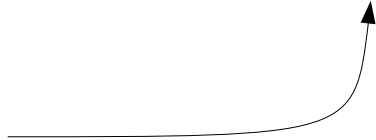

How to add a new goal

```
DEF_GOAL (EQ_MINUS, 3, "eq-", { r = v2 - (v0 == v1); })
```

Format:

```
DEF_GOAL (unique id, #args, "name", { C code; })
```

```
r    result  
v0   argument 1  
v1   argument 2  
...
```



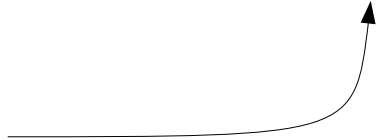
How to add a new goal

```
DEF_GOAL (EQ_MINUS, 3, "eq-", { r = v2 - (v0 == v1); })
```

Format:

```
DEF_GOAL (unique id, #args, "name", { C code; })
```

```
r    result  
v0   argument 1  
v1   argument 2  
...
```



Using the new goal:

```
$ make all  
$ ./superopt-avr -fname
```

How to add a new architecture

How to add a new architecture

Define the implementation in `superopt.h`

- Name, types (bitwidth)

How to add a new architecture

Define the implementation in `superopt.h`

- Name, types (bitwidth)
- “Unusual” instructions

```
#ifndef PERFORM_AND
#define PERFORM_AND(d, co, r1, r2, ci) \
    ((d) = (r1) & (r2), (co) = (ci))
#endif
```

How to add a new architecture




Define the implementation in `superopt.h`

- Name, types (bitwidth)
- “Unusual” instructions

```
#ifndef PERFORM_AND
#define PERFORM_AND(d, co, r1, r2, ci) \
    ((d) = (r1) & (r2), (co) = (ci))
#endif
```

- Also add mnemonic into `insn.def`

```
DEF_INSN (AND, 'b', "and")
```

Identifier   Name 
Type (binary, unary, etc)

How to add a new architecture

How to add a new architecture

To enable output in native assembler

How to add a new architecture

To enable output in native assembler

Extend `output_assembly`

- Register names
- Disassembly code

How to add a new architecture

To enable output in native assembler

Extend `output_assembly`

- Register names
- Disassembly code

```
case ADD_CO:
    printf("add      %s, %s", NAME(s1), NAME(s2)); break;
case ADD_CIO:
    printf("adc     %s, %s", NAME(s1), NAME(s2)); break;
```

How to add a new architecture

How to add a new architecture

`SYNTH (. . .)` in `synth.def`

How to add a new architecture

`SYNTH (. . .)` in `synth.def`

- Where the magic happens

How to add a new architecture

`SYNTH (. . .)` in `synth.def`

- Where the magic happens
- Loops over all the registers and all the instructions

How to add a new architecture

`SYNTH (. . .)` in `synth.def`

- Where the magic happens
- Loops over all the registers and all the instructions
- Use the macros for performing the instruction

How to add a new architecture

`SYNTH (. . .)` in `synth.def`

- Where the magic happens
- Loops over all the registers and all the instructions
- Use the macros for performing the instruction
- Then recurses (next level of iterative deepening)

How to add a new architecture

`SYNTH (. . .)` in `synth.def`

- Where the magic happens
- Loops over all the registers and all the instructions
- Use the macros for performing the instruction
- Then recurses (next level of iterative deepening)
- Add architecture entries for standard & custom instructions

How to add a new architecture

SYNTH (. . .) in synth.def

- Where the magic happens
- Loops over all the registers and all the instructions
- Use the macros for performing the instruction
- Then recurses (next level of iterative deepening)
- Add architecture entries for standard & custom instructions

```
#if SPARC || M88000
    /* sparc:          addx
       m88000:        addu.ci */
    PERFORM_ADD_CI(v, co, r1, r2, ci);
    RECURSE(ADD_CI, s1, s2, prune_hint & ~CY_JUST_SET);
#endif
```

How to add a new architecture

```
#if SPARC || M88000
    /* sparc:          addx
       m88000:        addu.ci */
    PERFORM_ADD_CI(v, co, r1, r2, ci);
    RECURSE(ADD_CI, s1, s2, prune_hint & ~CY_JUST_SET);
#endif
```

How to add a new architecture

```
#if SPARC || M88000
    /* sparc:          addx
       m88000:        addu.ci */
    PERFORM_ADD_CI(v, co, r1, r2, ci);
    RECURSE(ADD_CI, s1, s2, prune_hint & ~CY_JUST_SET);
#endif
```

Identifier _____
(insn.def)



How to add a new architecture

```
#if SPARC || M88000
    /* sparc:          addx
       m88000:        addu.ci */
    PERFORM_ADD_CI(v, co, r1, r2, ci);
    RECURSE(ADD_CI, s1, s2, prune_hint & ~CY_JUST_SET);
#endif
```

Identifier
(insn.def)

Registers
used

How to add a new architecture

```
#if SPARC || M88000
    /* sparc:          addx
       m88000:        addu.ci */
    PERFORM_ADD_CI(v, co, r1, r2, ci);
    RECURSE(ADD_CI, s1, s2, prune_hint & ~CY_JUST_SET);
#endif
```

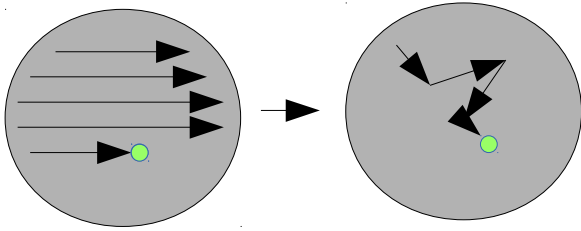
Identifier
(insn.def)

Registers
used

Speed hints.
(we didn't just set the carry)

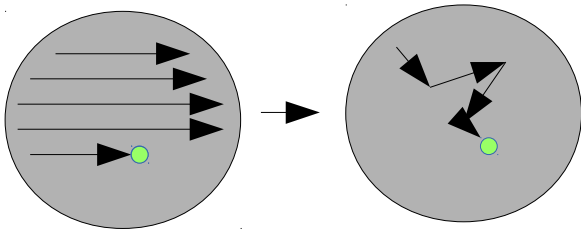
Our plans to extend GSO

Our plans to extend GSO

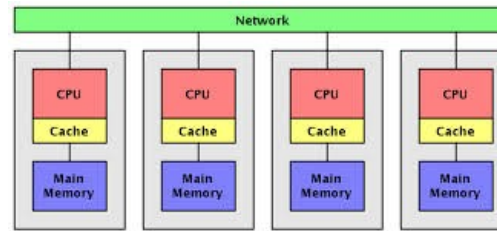


Machine learning

Our plans to extend GSO

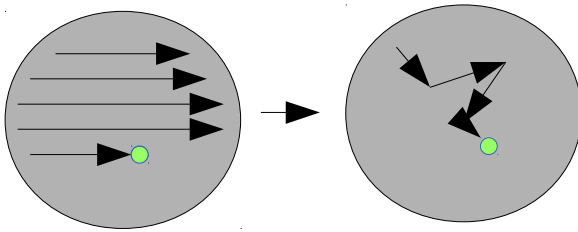


Machine learning

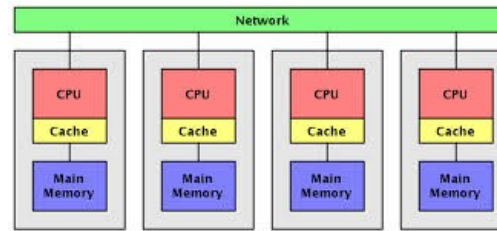


Parallelism

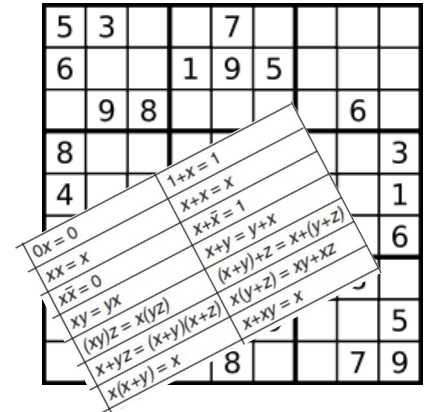
Our plans to extend GSO



Machine learning

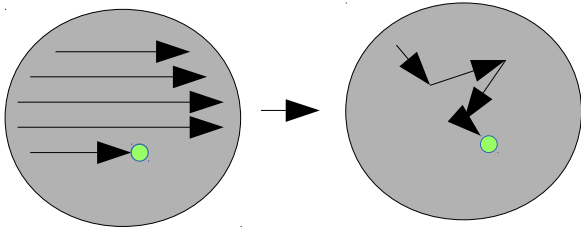


Parallelism

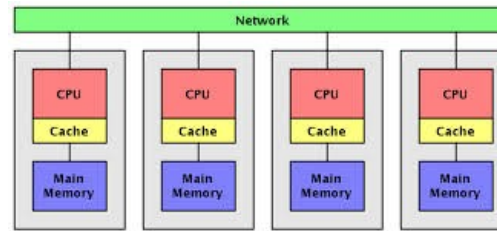


Instruction sequence verification

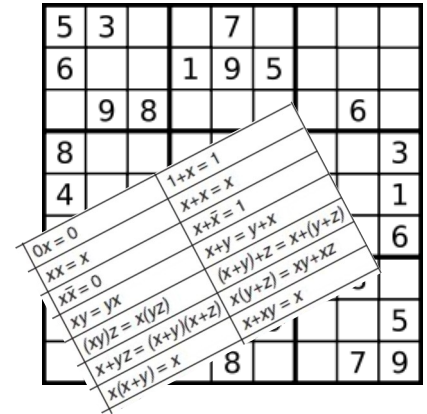
Our plans to extend GSO



Machine learning

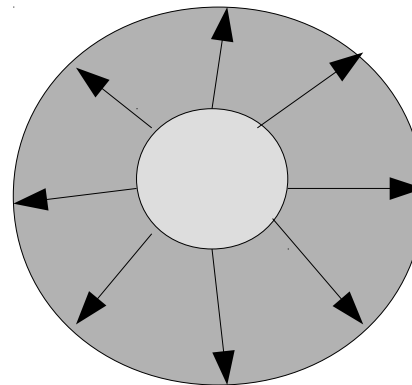


Parallelism

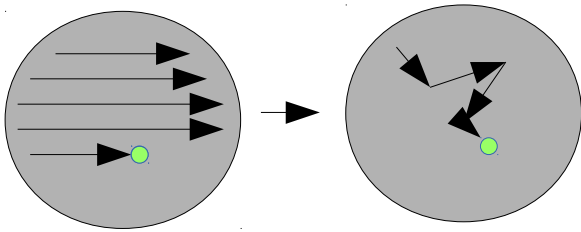


Instruction sequence verification

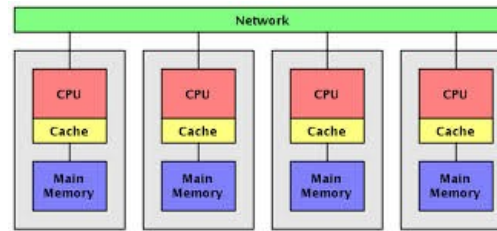
More instruction types



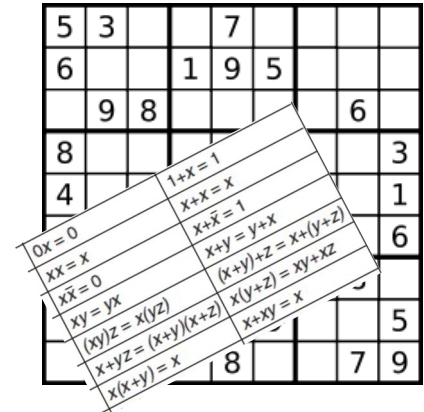
Our plans to extend GSO



Machine learning



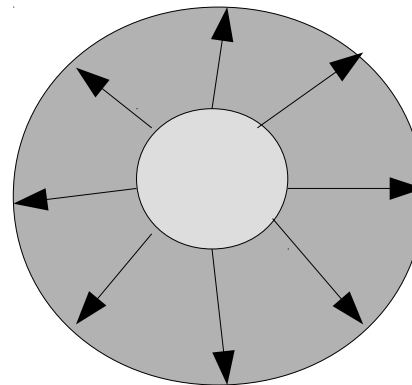
Parallelism



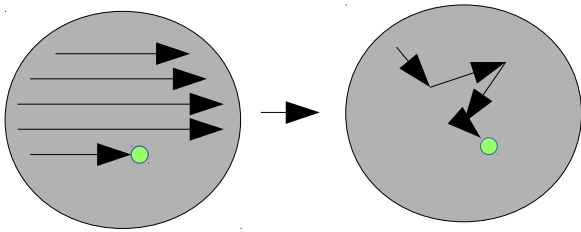
Instruction sequence verification

More instruction types

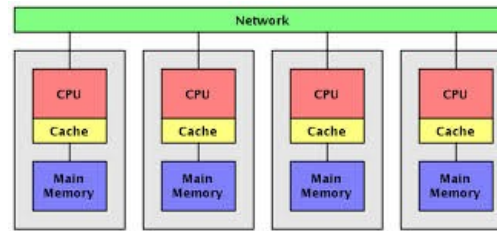
Memory access



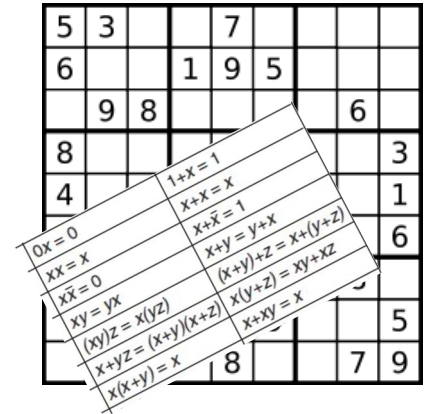
Our plans to extend GSO



Machine learning



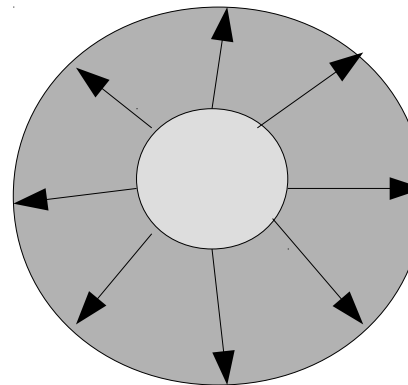
Parallelism



Instruction sequence verification

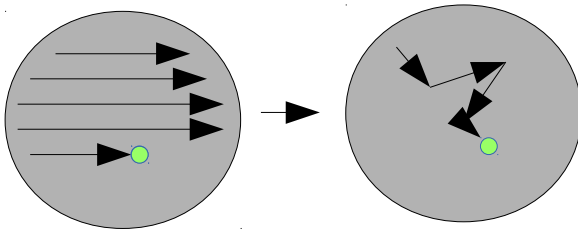
More instruction types

Memory access

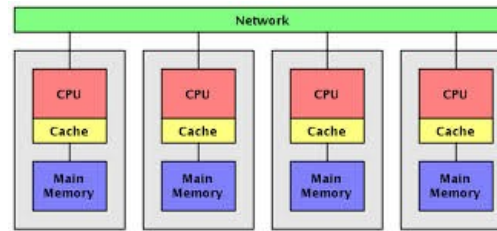


Floating point

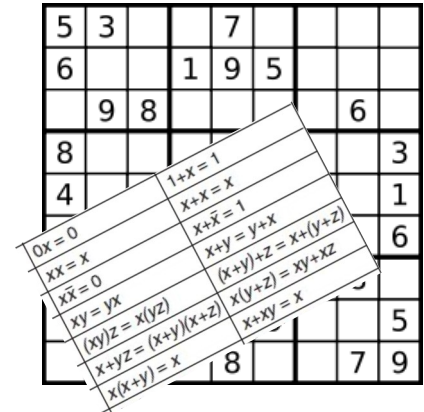
Our plans to extend GSO



Machine learning



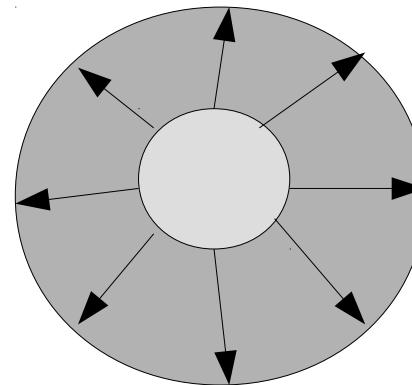
Parallelism



Instruction sequence verification

More instruction types

Memory access



Floating point

Multiple outputs

Thank You

Thank You

Superoptimization works

Thank You

Superoptimization works

New techniques are making it better

Thank You

Superoptimization works

New techniques are making it better

Lots of free software and tools

Thank You

Superoptimization works

New techniques are making it better

Lots of free software and tools



Thank You

Superoptimization works

New techniques are making it better

Lots of free software and tools

Try it yourself

github.com/embecosm/gnu-superopt

